

Supersymmetry at ATLAS

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Supersymmetry



- Supersymmetry (SUSY) fundamental continuous symmetry connecting fermions and bosons

$$Q_\alpha |F\rangle = |B\rangle, \quad Q_\alpha |B\rangle = |F\rangle$$

- $\{Q_\alpha, Q_\beta\} = -2\gamma^\mu_{\alpha\beta} p_\mu$: generators of SUSY ~ ‘square-root’ of translations

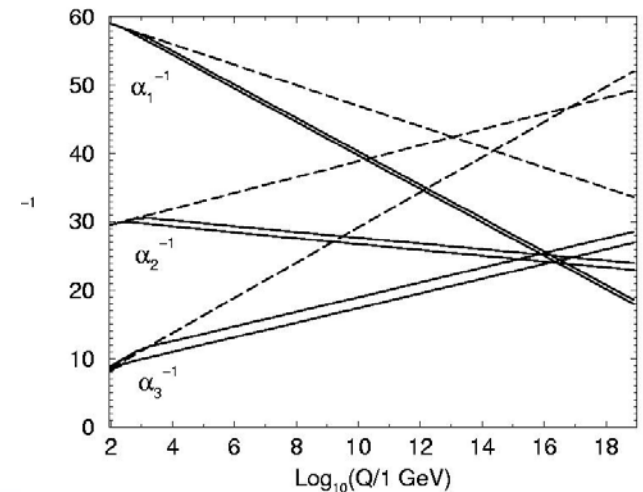
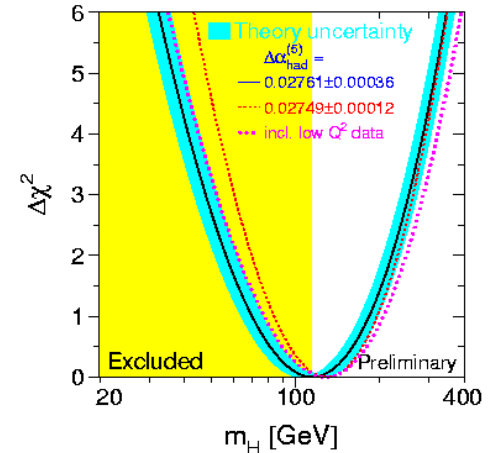
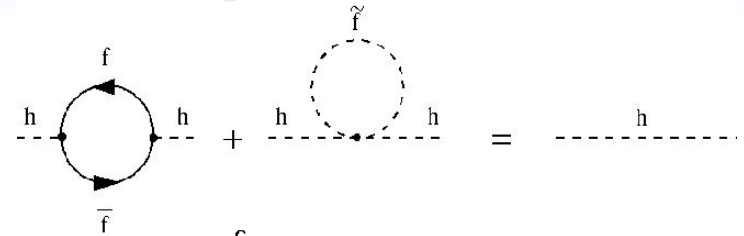
- Connection to space-time symmetry

- SUSY stabilises Higgs mass against loop corrections (gauge hierarchy/fine-tuning problem)

- Leads to Higgs mass ≤ 135 GeV

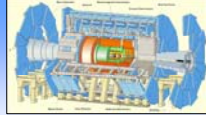
- Good agreement with LEP constraints from EW global fits

- SUSY modifies running of SM gauge couplings ‘just enough’ to give Grand Unification at single scale.





SUSY Spectrum



- SUSY gives rise to partners of SM states with opposite spin-statistics but otherwise same Quantum Numbers.

- Expect SUSY partners to have same masses as SM states

- Not observed (despite best efforts!)
- SUSY must be a broken symmetry at low energy

- Higgs sector also expanded

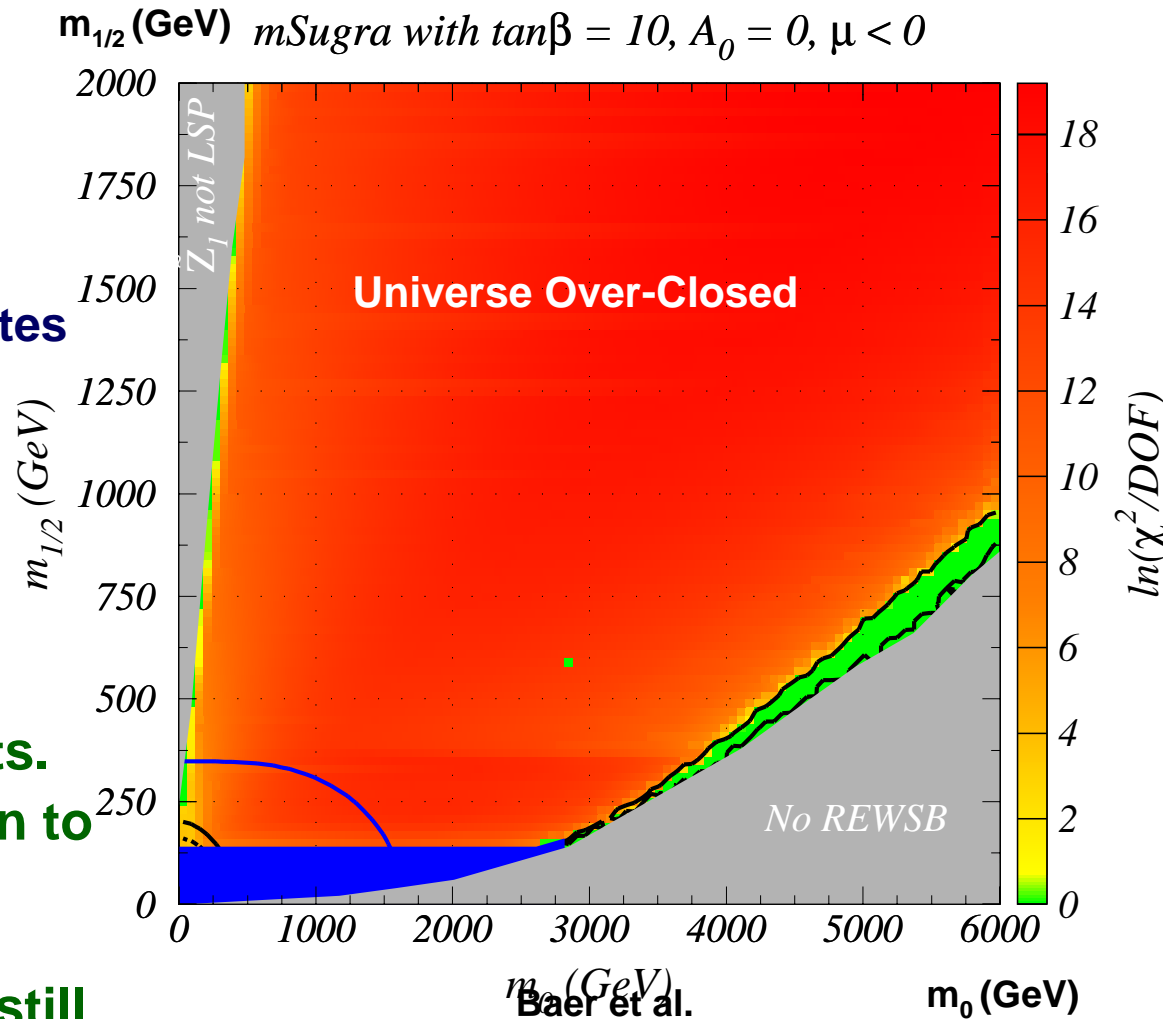
Standard Model Particles		SUSY Partners		
Particles	States	Sparticles	States	Mixtures
quarks (q) (spin- $\frac{1}{2}$)	$\begin{pmatrix} u \\ d \end{pmatrix}_L, u_R, d_R$ $\begin{pmatrix} c \\ s \end{pmatrix}_L, c_R, s_R$ $\begin{pmatrix} t \\ b \end{pmatrix}_L, t_R, b_R$	squarks (\tilde{q}) (spin-0)	$\begin{pmatrix} \tilde{u} \\ \tilde{d} \end{pmatrix}_L, \tilde{u}_R, \tilde{d}_R$ $\begin{pmatrix} \tilde{c} \\ \tilde{s} \end{pmatrix}_L, \tilde{c}_R, \tilde{s}_R$ $\begin{pmatrix} \tilde{t} \\ \tilde{b} \end{pmatrix}_L, \tilde{t}_R, \tilde{b}_R$	$\tilde{t}_{1,2}, \tilde{b}_{1,2}$
leptons (l) (spin- $\frac{1}{2}$)	$\begin{pmatrix} e \\ \nu_e \end{pmatrix}_L, e_R$ $\begin{pmatrix} \mu \\ \nu_\mu \end{pmatrix}_L, \mu_R$ $\begin{pmatrix} \tau \\ \nu_\tau \end{pmatrix}_L, \tau_R$	sleptons (\tilde{l}) (spin-0)	$\begin{pmatrix} \tilde{e} \\ \tilde{\nu}_e \end{pmatrix}_L, \tilde{e}_R$ $\begin{pmatrix} \tilde{\mu} \\ \tilde{\nu}_\mu \end{pmatrix}_L, \tilde{\mu}_R$ $\begin{pmatrix} \tilde{\tau} \\ \tilde{\nu}_\tau \end{pmatrix}_L, \tilde{\tau}_R$	$\tilde{\tau}_{1,2}$
gauge/Higgs bosons (spin-1, spin-0)	g, Z, γ, h, H, A W^\pm, H^\pm	gauginos/Higgsinos (spin- $\frac{1}{2}$)	$\tilde{g}, \tilde{Z}, \tilde{\gamma}, \tilde{H}_{1,2}^0$ $\tilde{W}^\pm, \tilde{H}^\pm$	$\tilde{\chi}_{1,2,3,4}^0$ $\tilde{\chi}_{1,2}^\pm$
graviton (spin-2)	G	gravitino (spin- $\frac{3}{2}$)	\tilde{G}	



SUSY & Dark Matter



- R-Parity $R_p = (-1)^{3B+2S+L}$
- Conservation of R_p (motivated e.g. by string models) attractive
 - e.g. protects proton from rapid decay via SUSY states
- Causes Lightest SUSY Particle (LSP) to be absolutely stable
- LSP neutral/weakly interacting to escape astroparticle bounds on anomalous heavy elements.
- Naturally provides solution to dark matter problem of astrophysics / cosmology
- R-Parity violating models still possible → not covered here.

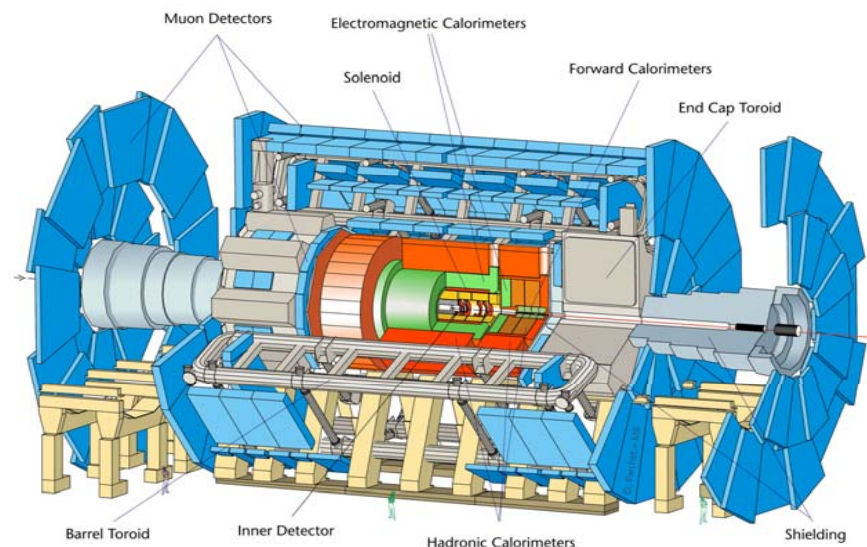




SUSY @ ATLAS



- LHC will be a 14 TeV proton-proton collider located inside the LEP tunnel at CERN.
- Luminosity goals:
 - 10 fb⁻¹ / year (first 3 years)
 - 100 fb⁻¹/year (subsequently).
- First data in 2007.
- Higgs & SUSY main goals.



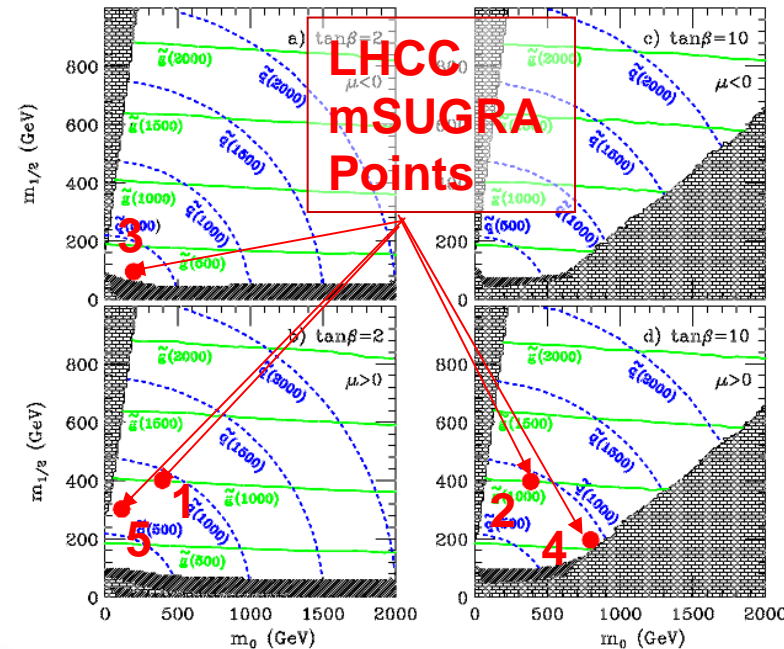
- Much preparatory work carried out historically by ATLAS
 - Summarised in Detector and Physics Performance TDR (1998/9).
- Work continuing to ensure ready to test new ideas in 2007.
- Concentrate here on more recent work.



Model Framework



- Minimal Supersymmetric Extension of the Standard Model (MSSM) contains > 105 free parameters, NMSSM etc. has more \rightarrow difficult to map complete parameter space!
- Assume specific well-motivated model framework in which generic signatures can be studied.
- Often assume SUSY broken by gravitational interactions \rightarrow mSUGRA/CMSSM framework : unified masses and couplings at the GUT scale \rightarrow 5 free parameters ($m_0, m_{1/2}, A_0, \tan(\beta), \text{sgn}(\mu)$).
- R-Parity assumed to be conserved.
- Exclusive studies use benchmark points in mSUGRA parameter space:
 - LHCC Points 1-6;
 - Post-LEP benchmarks (Battaglia et al.);
 - Snowmass Points and Slopes (SPS);
 - etc...

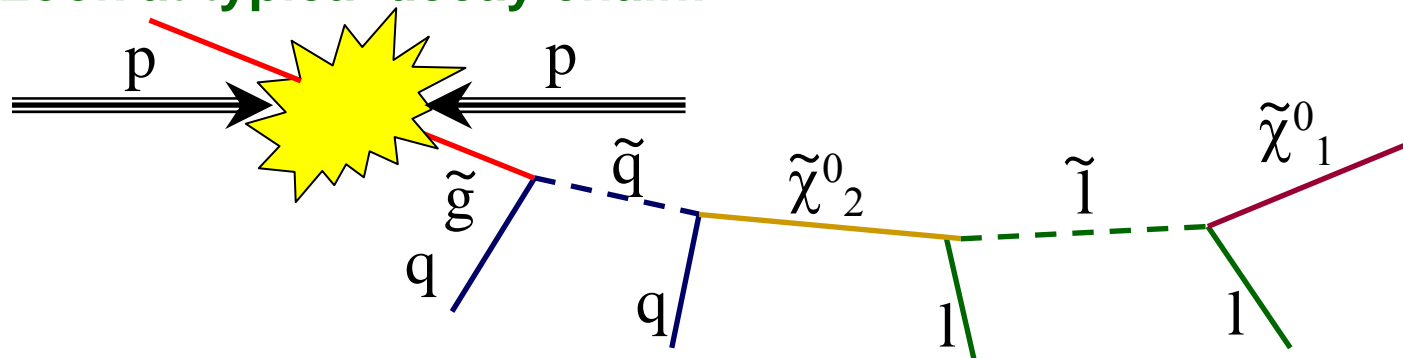




SUSY Signatures



- **Q: What do we expect SUSY events @ LHC to look like?**
- **A: Look at typical decay chain:**



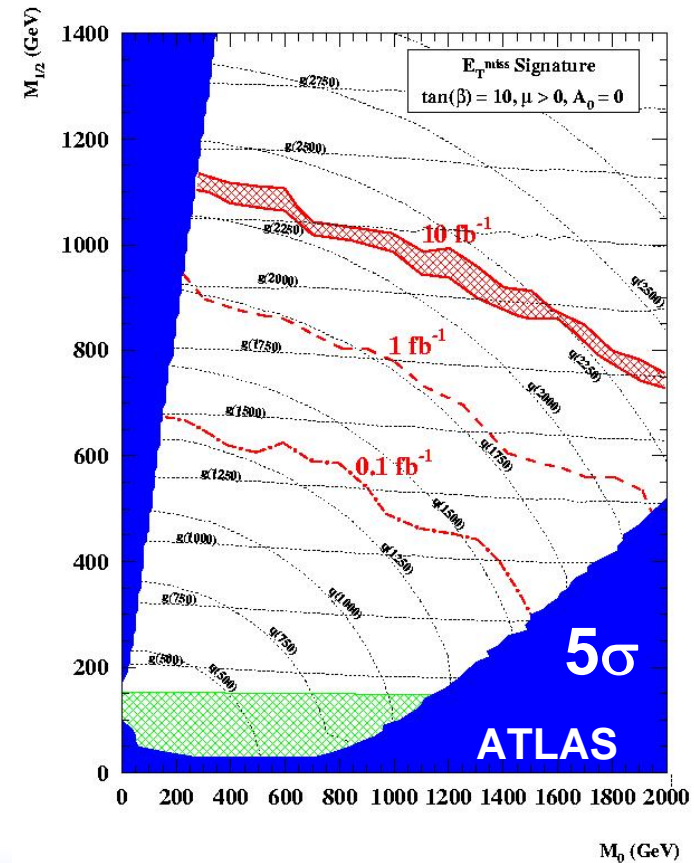
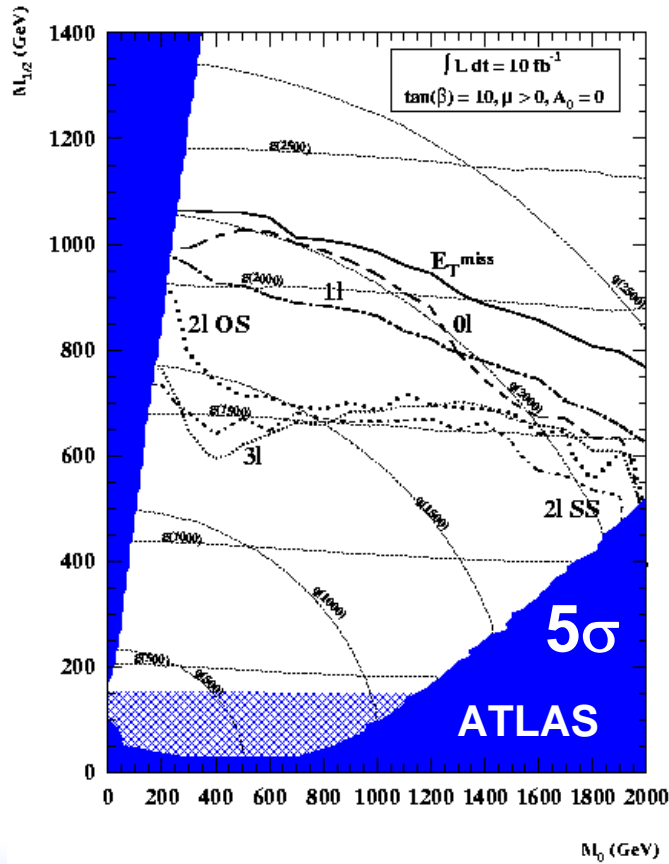
- **Strongly interacting sparticles (squarks, gluinos) dominate production.**
- **Heavier than sleptons, gauginos etc. → cascade decays to LSP.**
- **Long decay chains and large mass differences between SUSY states**
 - **Many high p_T objects observed (leptons, jets, b-jets).**
- **If R-Parity conserved LSP (lightest neutralino in mSUGRA) stable and sparticles pair produced.**
 - **Large E_T^{miss} signature (c.f. $W \rightarrow l\nu$).**
- **Closest equivalent SM signature $t \rightarrow Wb$.**



Inclusive Searches



- Use 'golden' Jets + n leptons + E_T^{miss} discovery channel.
- Map statistical discovery reach in mSUGRA m_0 - $m_{1/2}$ parameter space.
- Sensitivity only weakly dependent on A_0 , $\tan(\beta)$ and $\text{sign}(\mu)$.
- Syst.+ stat. reach harder to assess: focus of current & future work.



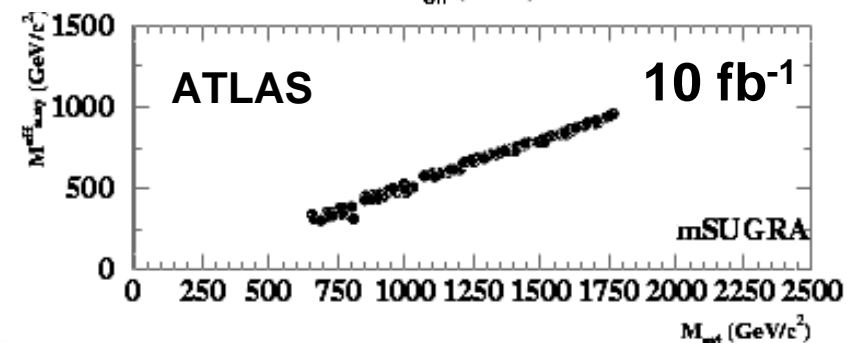
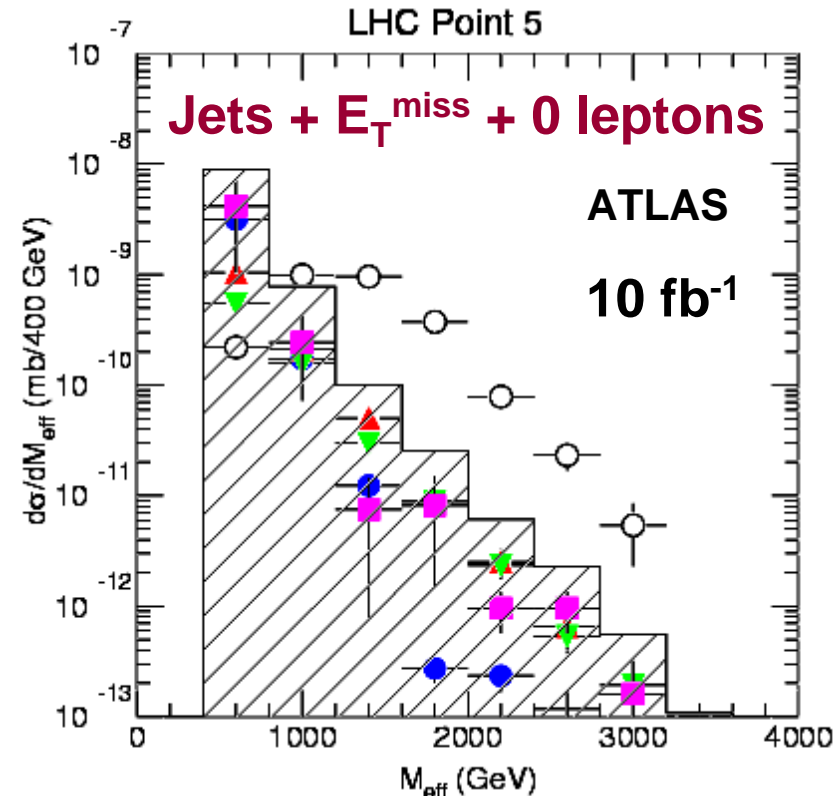


SUSY Mass Scale



- First measured SUSY parameter likely to be mass scale:
 - Defined as weighted mean of masses of initial sparticles.
- Calculate distribution of 'effective mass' variable defined as scalar sum of masses of all jets (or four hardest) and E_T^{miss} :

$$M_{\text{eff}} = \sum |p_T^i| + E_T^{\text{miss}}.$$
- Distribution peaked at \sim twice SUSY mass scale for signal events.
- Pseudo 'model-independent' measurement.
- Typical measurement error (syst+stat) \sim 10% for mSUGRA models for 10 fb^{-1} .

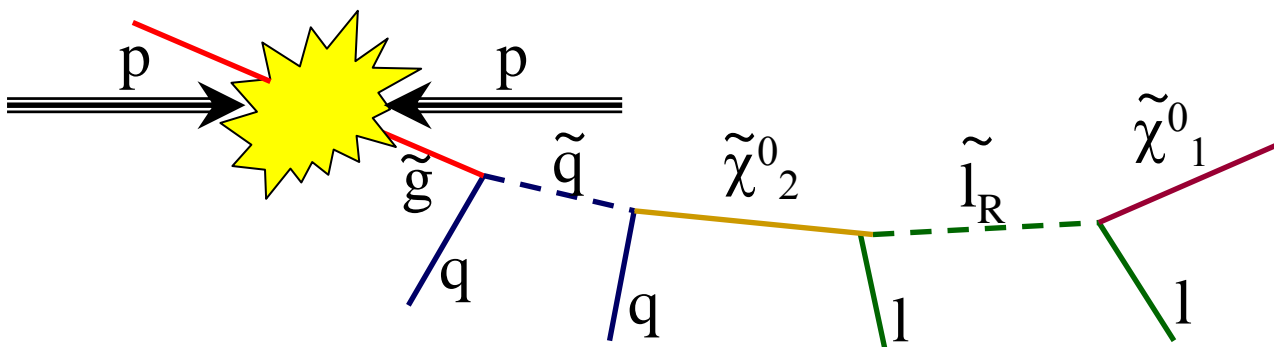




Exclusive Studies



- With more data will attempt to measure weak scale SUSY parameters (masses etc.) using exclusive channels.
- Different philosophy to TeV Run II (better S/B, longer decay chains) → aim to use model-independent measures.



- Two neutral LSPs escape from each event
 - Impossible to measure mass of each sparticle using one channel alone
- Use kinematic end-points to measure combinations of masses.
- Old technique used many times before (ν mass from β decay spectrum, W (transverse) mass in $W \rightarrow l\nu$).
- Difference here is we don't know mass of neutral final state particles.

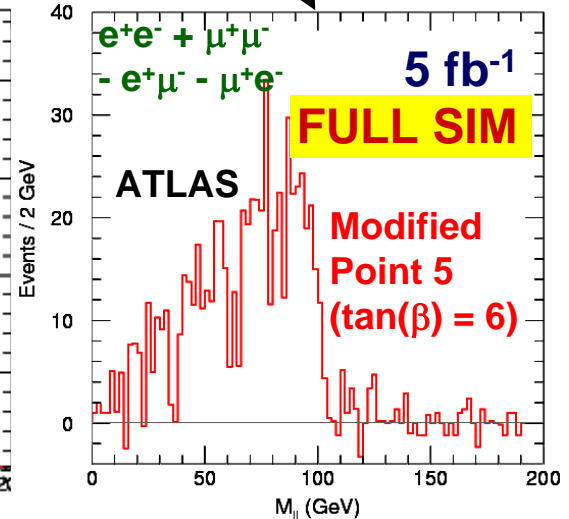
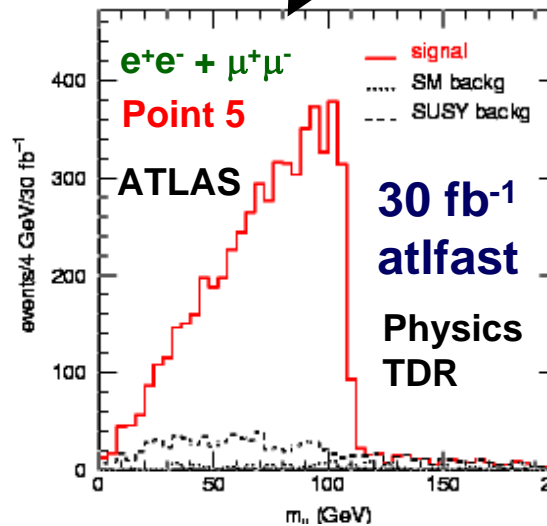
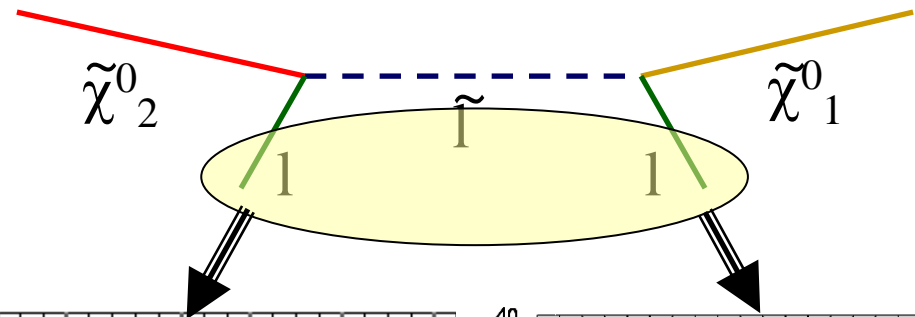


Dilepton Edge Measurements

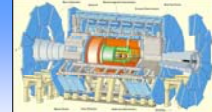


- When kinematically accessible $\tilde{\chi}_2^0$ can undergo sequential two-body decay to $\tilde{\chi}_1^0$ via a right-slepton (e.g. LHC Point 5).
- Results in sharp OS SF dilepton invariant mass edge sensitive to combination of masses of sparticles.
- Can perform SM & SUSY background subtraction using OF distribution

$$e^+e^- + \mu^+\mu^- - e^+\mu^- - \mu^+e^-$$
- Position of edge measured with **precision ~ 0.5%** (30 fb⁻¹).

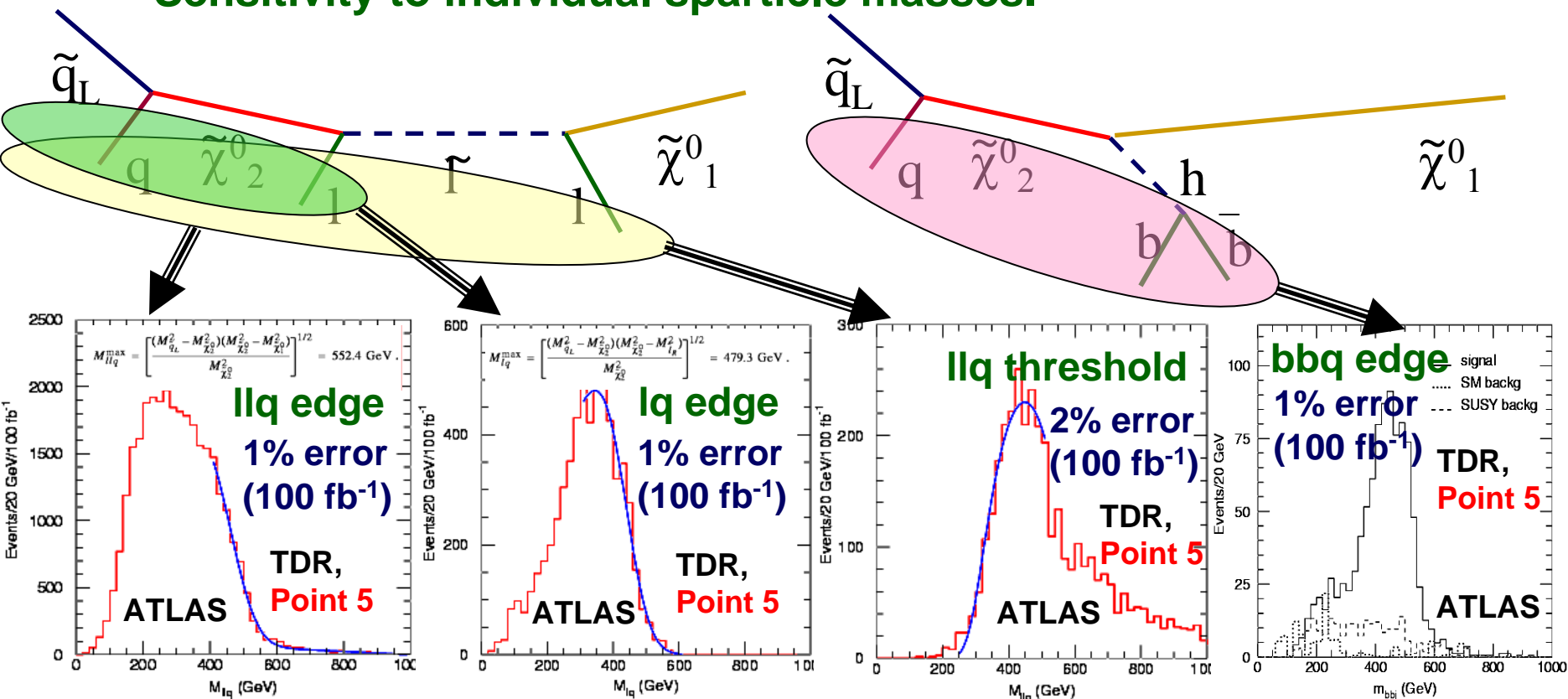


$$M_{ll}^{\max} = M(\tilde{\chi}_2^0) \sqrt{1 - \frac{M^2(\tilde{l}_R)}{M^2(\tilde{\chi}_2^0)}} \sqrt{1 - \frac{M^2(\tilde{\chi}_1^0)}{M^2(\tilde{l}_R)}} = 108.93 \text{ GeV}$$



Measurements With Squarks

- Dilepton edge starting point for reconstruction of decay chain.
- Make invariant mass combinations of leptons and jets.
- Gives multiple constraints on combinations of four masses.
- Sensitivity to individual sparticle masses.





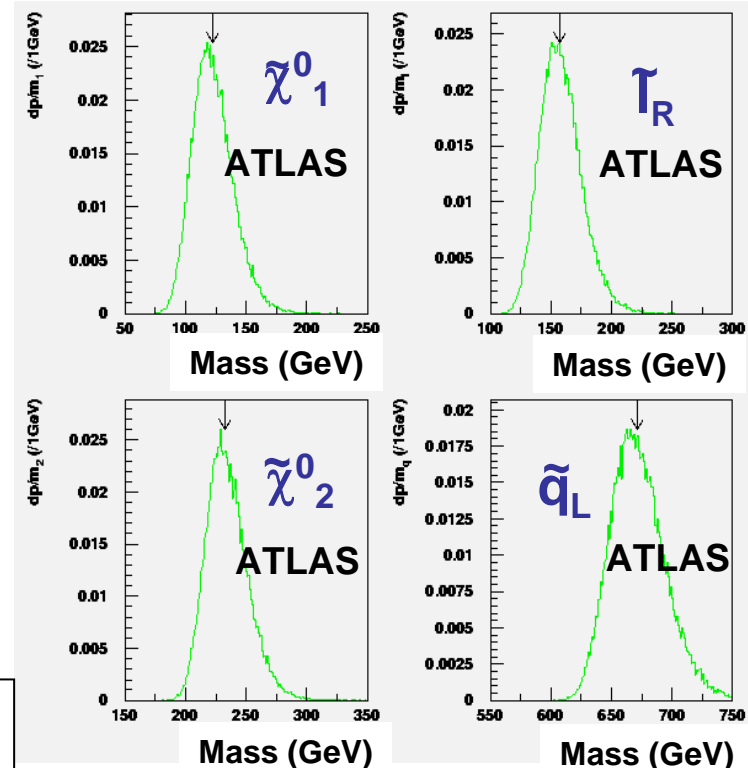
'Model-Independent' Masses



- Combine measurements from edges from different jet/lepton combinations to obtain 'model-independent' mass measurements.

Related edge	Kinematic endpoint
l^+l^- edge	$(m_{ll}^{\max})^2 = (\xi - \tilde{l})(\tilde{l} - \bar{\chi})/\tilde{l}$
l^+l^-q edge	$(m_{llq}^{\max})^2 = \begin{cases} \max \left[\frac{(\bar{q}-\xi)(\xi-\tilde{l})}{\xi}, \frac{(\bar{q}-\tilde{l})(\tilde{l}-\bar{\chi})}{\tilde{l}}, \frac{(\bar{q}-\xi)(\xi-\tilde{l})}{\tilde{l}} \right] \\ \text{except for the special case in which } \tilde{l}^2 < \bar{q}\tilde{\chi} < \xi^2 \text{ and} \\ \xi^2\tilde{\chi} < \bar{q}\tilde{l}^2 \text{ where one must use } (m_{lq}^{\max} - m_{\tilde{l}q}^{\max})^2. \end{cases}$
Xq edge	$(m_{Xq}^{\max})^2 = X + (\bar{q} - \xi) \left[\xi + X - \tilde{\chi} + \sqrt{(\xi - X - \tilde{\chi})^2 - 4X\tilde{\chi}} \right] / (2\xi)$
l^+l^-q threshold	$(m_{llq}^{\min})^2 = \begin{cases} [2\tilde{l}(\bar{q} - \xi)(\xi - \tilde{\chi}) + (\bar{q} + \xi)(\xi - \tilde{l})(\tilde{l} - \bar{\chi}) \\ -(\bar{q} - \xi)\sqrt{(\xi + \tilde{l})^2(\tilde{l} + \bar{\chi})^2 - 16\xi\tilde{l}^2\tilde{\chi}}] / (4\xi) \end{cases}$
$l^+_{near}l^-$ edge	$(m_{near}^{\max})^2 = (\bar{q} - \xi)(\xi - \tilde{l})/\xi$
$l^{\pm}_{far}q$ edge	$(m_{farq}^{\max})^2 = (\bar{q} - \xi)(\tilde{l} - \bar{\chi})/\tilde{l}$
$l^{\pm}\tilde{q}$ high-edge	$(m_{l\tilde{q}}^{\max})^2 = \max \left[(m_{l\tilde{q}}^{\max})^2, (m_{l\tilde{q}}^{\max})^2 \right]$
$l^{\pm}\tilde{q}$ low-edge	$(m_{l\tilde{q}}^{\max})^2 = \min \left[(m_{l\tilde{q}}^{\max})^2, (\bar{q} - \xi)(\tilde{l} - \bar{\chi}) / (2\tilde{l} - \bar{\chi}) \right]$
M_{Z_2} edge	$\Delta M = m_{\tilde{q}} - m_{\tilde{\chi}_2^0}$

Table 4: The absolute kinematic endpoints of invariant mass quantities formed from decay chains of the types mentioned in the text for known particle masses. The following shorthand notation has been used: $\bar{\chi} = m_{\tilde{\chi}_1^0}$, $\tilde{l} = m_{\tilde{l}}$, $\xi = m_{\tilde{\chi}_2^0}$, $\bar{q} = m_{\tilde{q}}$ and X is $m_{\tilde{q}}$ or $m_{\tilde{l}}$ depending on which particle participates in the 'branched' decay.



LHCC Point 5

Sparticle	Expected precision (100 fb ⁻¹)
\tilde{q}_L	$\pm 3\%$
$\tilde{\chi}^0_2$	$\pm 6\%$
$\tilde{\tau}_R$	$\pm 9\%$
$\tilde{\chi}^0_1$	$\pm 12\%$



Sbottom/Gluino Mass



- Following measurement of squark, slepton and neutralino masses move up decay chain and study alternative chains.
- One possibility: require b-tagged jet in addition to dileptons.
- Give sensitivity to sbottom mass (actually two peaks) and gluino mass.
- Problem with large error on input $\tilde{\chi}^0_1$ mass remains \rightarrow reconstruct difference of gluino and sbottom masses.
- Allows separation of \tilde{b}_1 and \tilde{b}_2 with 300 fb^{-1} .

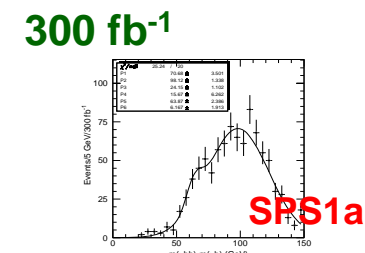
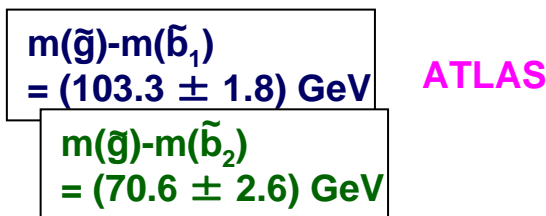
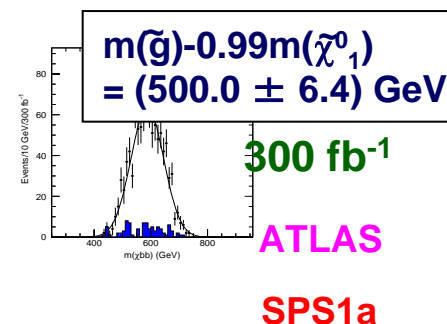
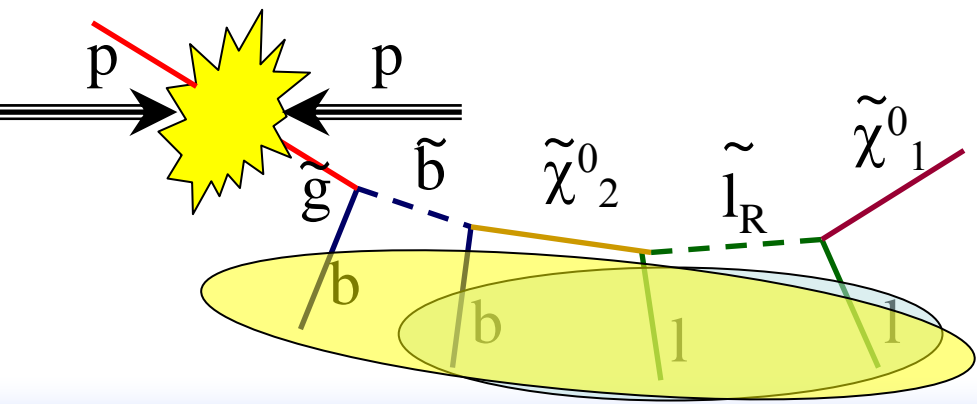


Figure 8: Distribution of $m(\tilde{\chi}^0_2) - m(\tilde{\chi}^0_1)$ for an integrated luminosity of 300 fb^{-1} . Superimposed is the fit performed assuming the sum of two gaussian distributions.

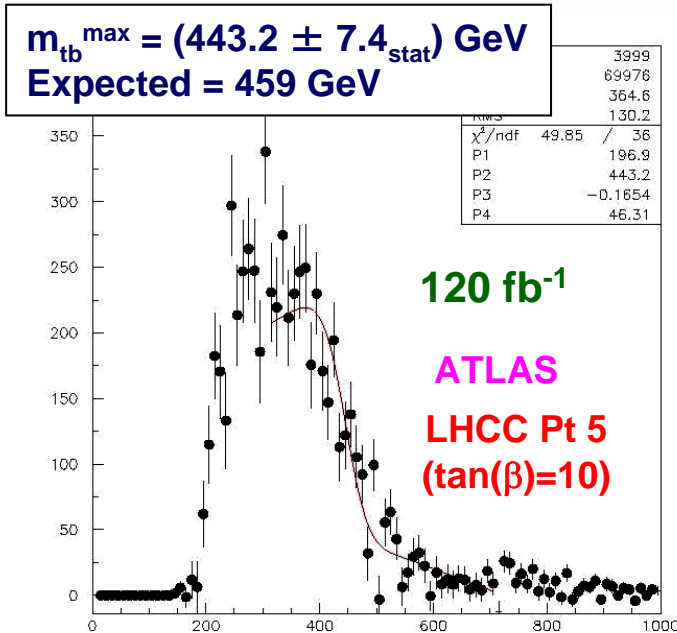
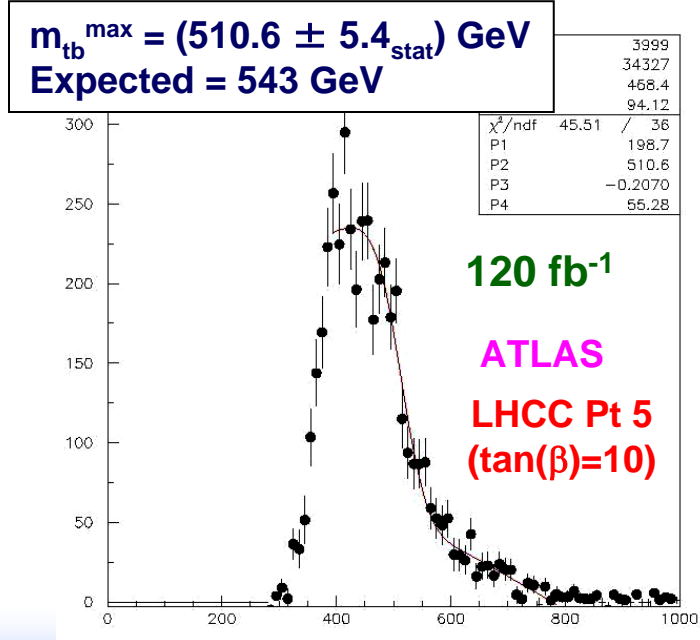




Stop Mass



- Look at edge in tb mass distribution.
- Contains contributions from
 - $\tilde{g} \rightarrow t\bar{t}_1 \rightarrow tb\tilde{\chi}_1^+$
 - $\tilde{g} \rightarrow b\bar{b}_1 \rightarrow bt\tilde{\chi}_1^+$
 - SUSY backgrounds
- Measures weighted mean of end-points
- Require $m(jj) \sim m(W)$, $m(jjb) \sim m(t)$



- Subtract sidebands from $m(jj)$ distribution
- Can use similar approach with $\tilde{g} \rightarrow t\bar{t}_1 \rightarrow tt\tilde{\chi}_i^0$
 - Di-top selection with sideband subtraction
- Also use 'standard' bll analyses (previous slide)

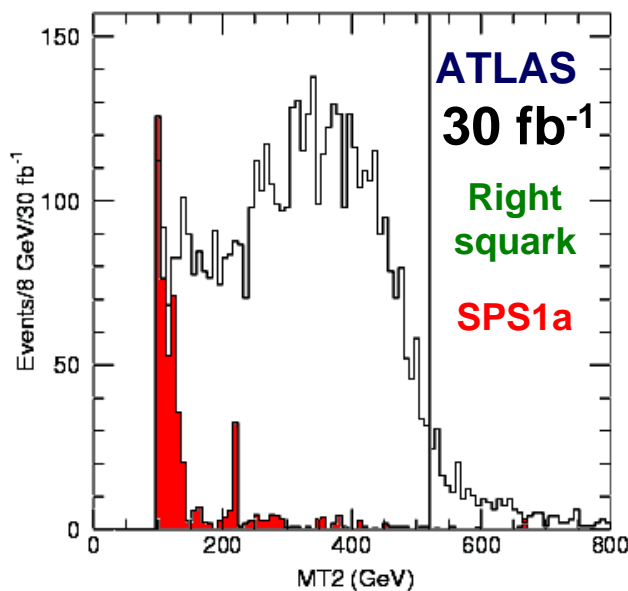
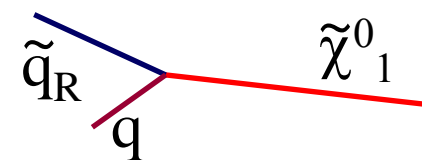


RH Squark Mass

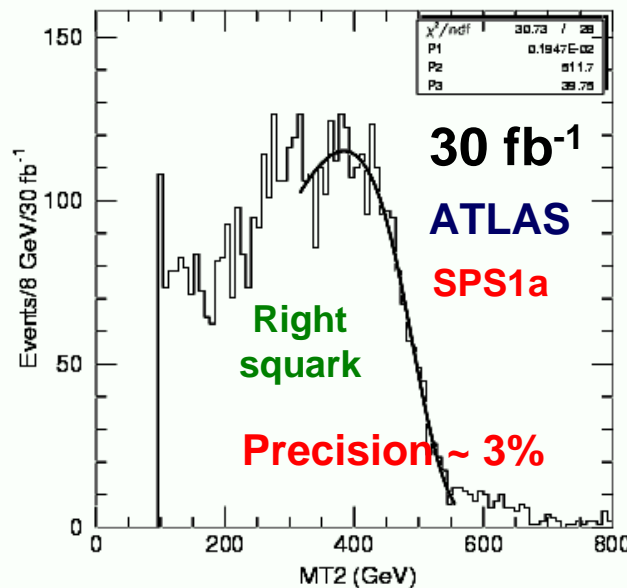


- Right handed squarks difficult as rarely decay via 'standard' $\tilde{\chi}^0_2$ chain
 - Typically BR ($\tilde{q}_R \rightarrow \tilde{\chi}^0_1 q$) > 99%.
- Instead search for events with 2 hard jets and lots of E_T^{miss} .
- Reconstruct mass using 'stransverse mass' (Allanach et al.):

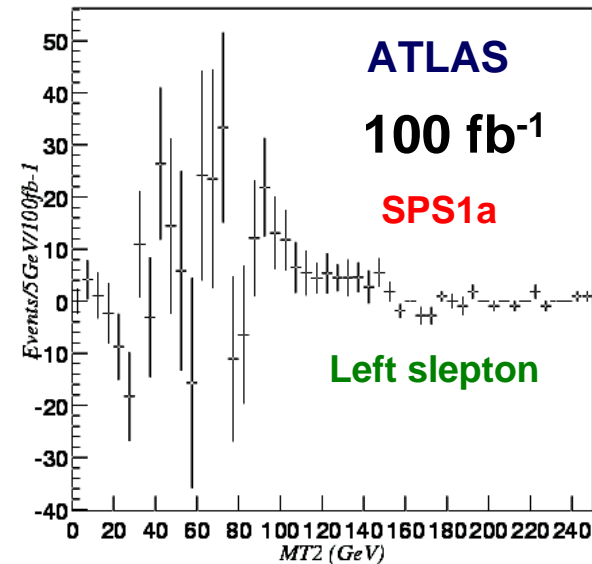
$$m_{T2}^2 = \min_{q_T^{\chi(1)} + q_T^{\chi(2)} = E_T^{\text{miss}}} [\max\{m_T^2(p_T^{j(1)}, q_T^{\chi(1)}; m_\chi), m_T^2(p_T^{j(2)}, q_T^{\chi(2)}; m_\chi)\}]$$
- Needs $\tilde{\chi}^0_1$ mass measurement as input.
- Also works for sleptons.



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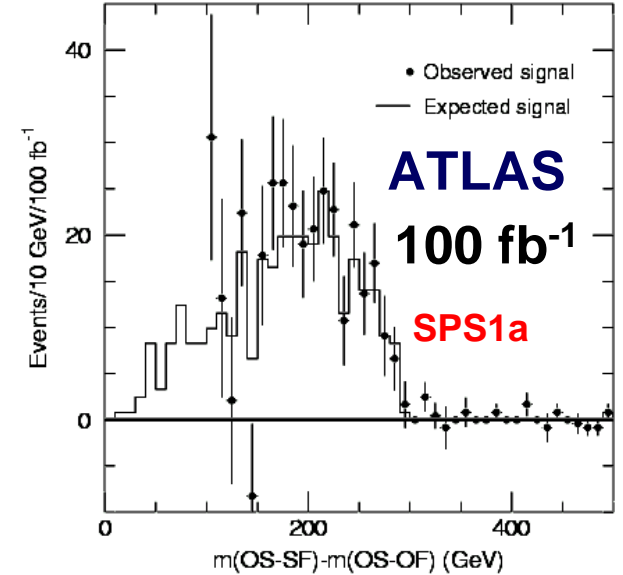
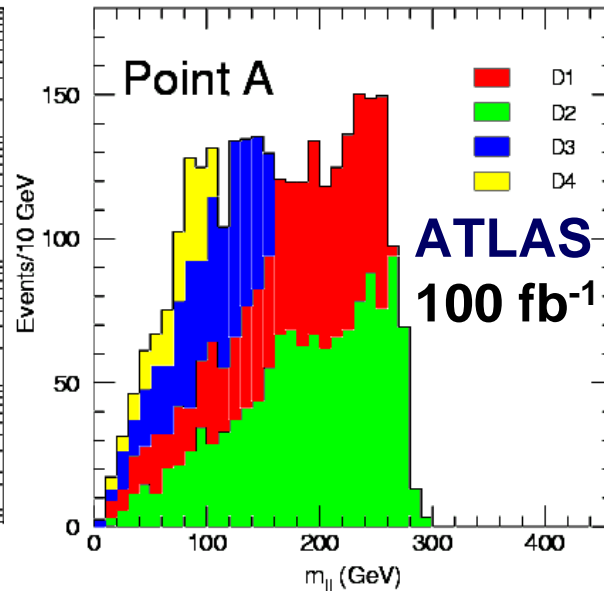
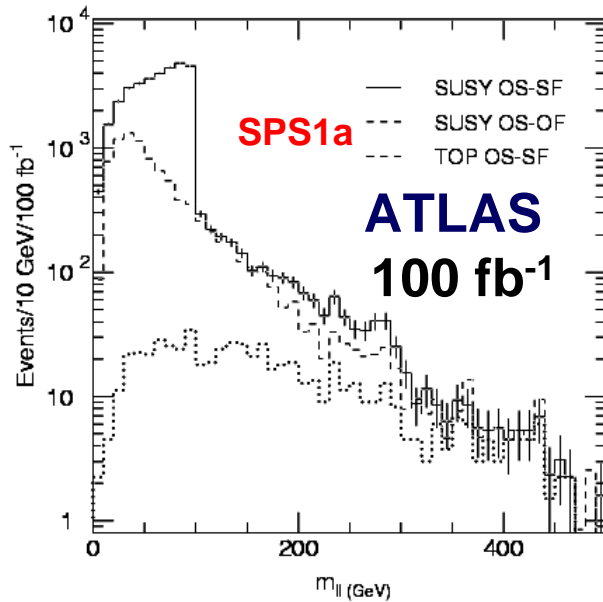
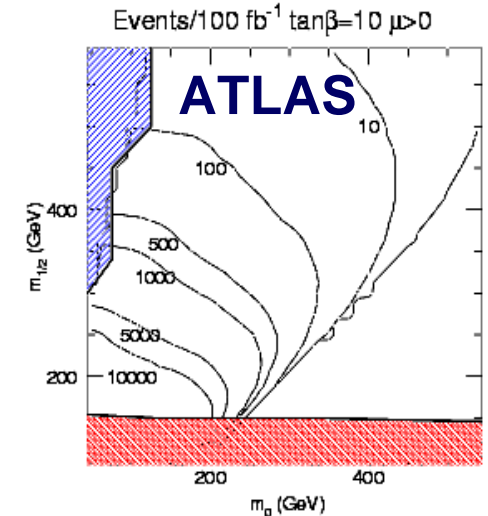


Heavy Gaugino Measurements



- Also possible to identify dilepton edges from decays of heavy gauginos.
- Requires high stats.
- Crucial input to reconstruction of MSSM neutralino mass matrix (independent of SUSY breaking scenario).

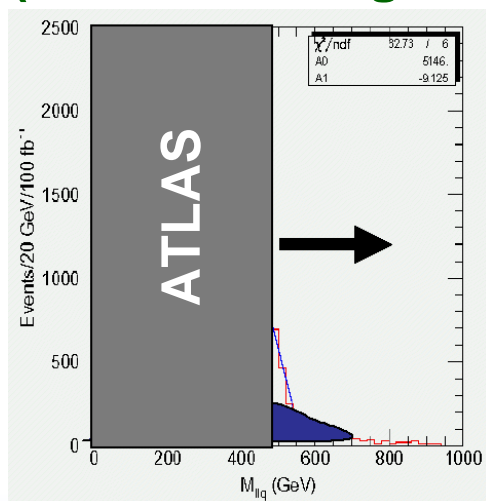
$\tilde{\chi}_4^0$



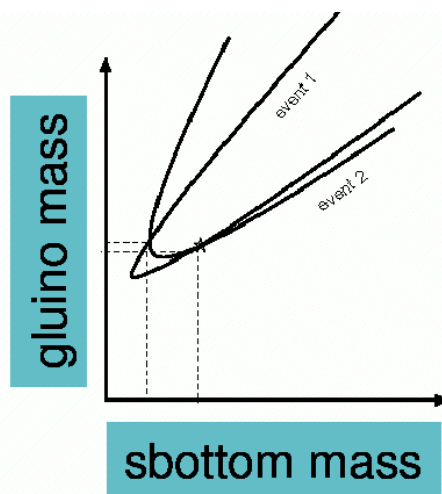


Mass Relation Method

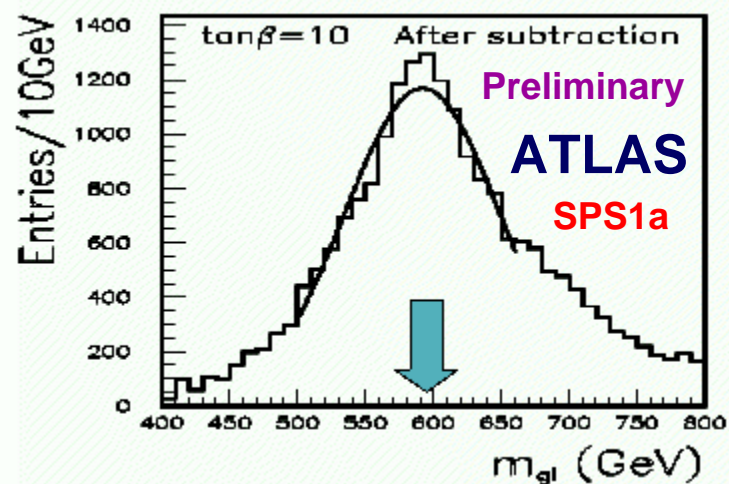
- New idea for reconstructing SUSY masses!
- ‘Impossible to measure mass of each sparticle using one channel alone’ (Slide 10).
 - Should have added caveat: Only if done event-by-event!
- Assume in each decay chain 5 inv. mass constraints for 6 unknowns (4 $\tilde{\chi}^0_1$ momenta + gluino mass + sbottom mass).
- Remove ambiguities by combining different events analytically \rightarrow ‘mass relation method’ (Nojiri et al.).
- Also allows all events to be used, not just those passing hard cuts (useful if background small, but stats limited – e.g. high scale SUSY).



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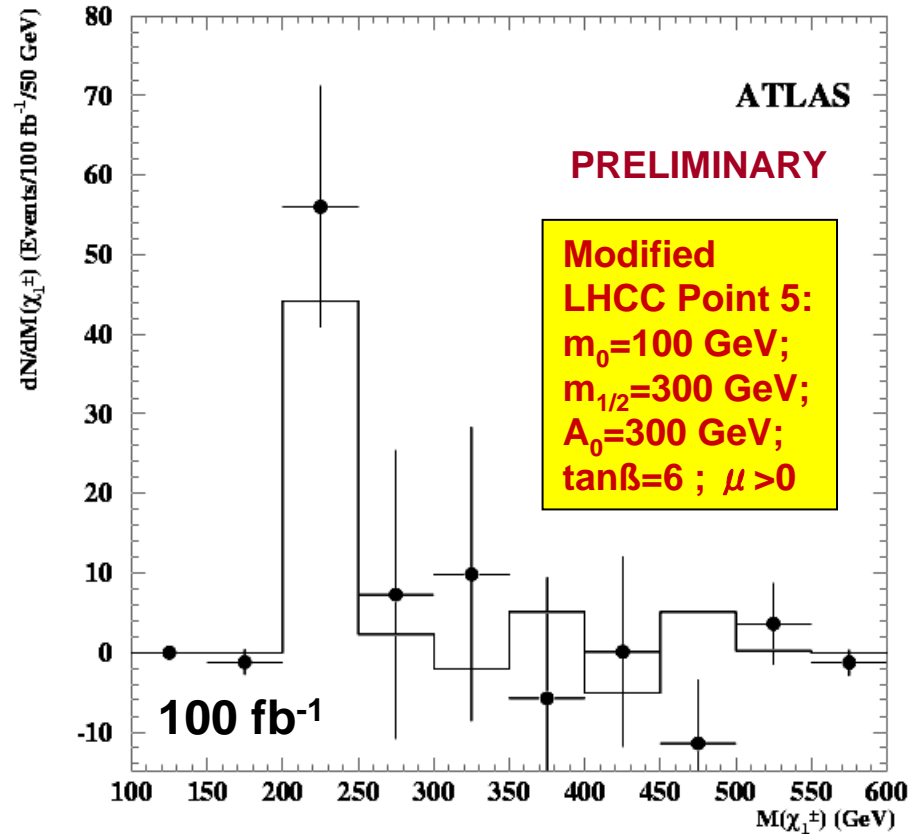
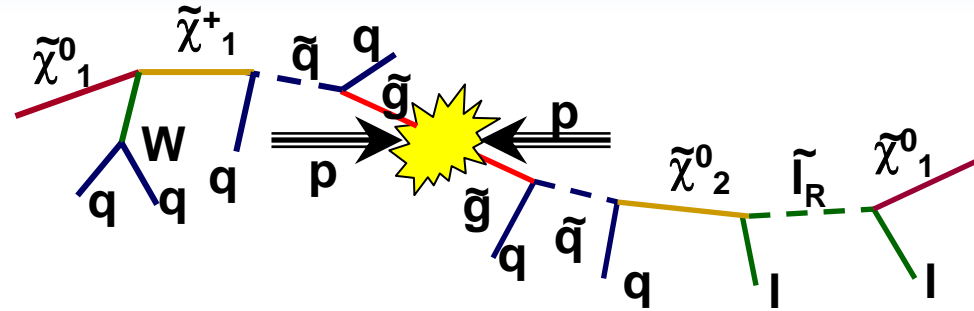
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Chargino Mass Measurement



- Mass of lightest chargino very difficult to measure as does not participate in standard dilepton SUSY decay chain.
- Decay process via ν +slepton gives too many extra degrees of freedom - concentrate instead on decay $\tilde{\chi}^+_{1} \rightarrow W \tilde{\chi}^0_{1}$.
- Require dilepton $\tilde{\chi}^0_{2}$ decay chain on other 'leg' of event and use kinematics to calculate chargino mass analytically.
- Using sideband subtraction technique obtain clear peak at true chargino mass (218 GeV).
- **~ 3 σ significance for 100 fb⁻¹.**



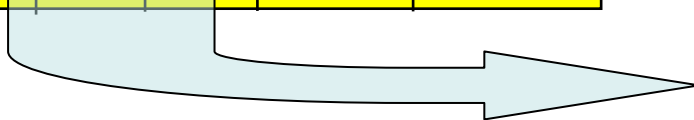


Measuring Model Parameters



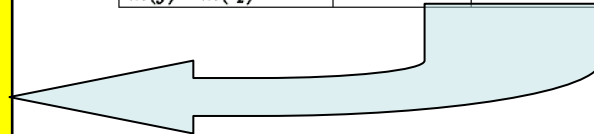
- Alternative use for SUSY observables (invariant mass end-points, thresholds etc.).
- Here assume mSUGRA/CMSSM model and perform global fit of model parameters to observables
 - So far mostly private codes but e.g. SFITTER, FITTINO now on the market;
 - c.f. global EW fits at LEP, ZFITTER, TOPAZ0 etc.

Point	m_0	$m_{1/2}$	A_0	$\tan(\beta)$	$\text{sign}(\mu)$
LHC Point 5	100	300	300	2	+1
SPS1a	100	250	-100	10	+1



Parameter	Expected precision (300 fb ⁻¹)
m_0	± 2%
$m_{1/2}$	± 0.6%
$\tan(\beta)$	± 9%
A_0	± 16%

Variable	Value (GeV)	Stat. (GeV)	Errors	
			Scale (GeV)	Total
$m_{\ell\ell}^{\text{max}}$	77.07	0.03	0.08	0.08
$m_{\ell\ell}^{\text{low}}$	428.5	1.4	4.3	4.5
$m_{\ell\ell}^{\text{high}}$	300.3	0.9	3.0	3.1
$m_{\ell\ell}^{\text{min}}$	378.0	1.0	3.8	3.9
$m_{\ell\ell}^{\text{min}}$	201.9	1.6	2.0	2.6
$m_{\ell\ell}^{\text{min}}$	183.1	3.6	1.8	4.1
$m(\ell_L) - m(\tilde{\chi}_1^0)$	106.1	1.6	0.1	1.6
$m_{\ell\ell}^{\text{max}}(\tilde{\chi}_1^0)$	280.9	2.3	0.3	2.3
$m_{\tau\tau}$	80.6	5.0	0.8	5.1
$m(\tilde{g}) - 0.99 \times m(\tilde{\chi}_1^0)$	500.0	2.3	6.0	6.4
$m(\tilde{g}_R) - m(\tilde{\chi}_1^0)$	424.2	10.0	4.2	10.9
$m(\tilde{g}) - m(\tilde{b}_1)$	103.3	1.5	1.0	1.8
$m(\tilde{g}) - m(\tilde{b}_2)$	70.6	2.5	0.7	2.6

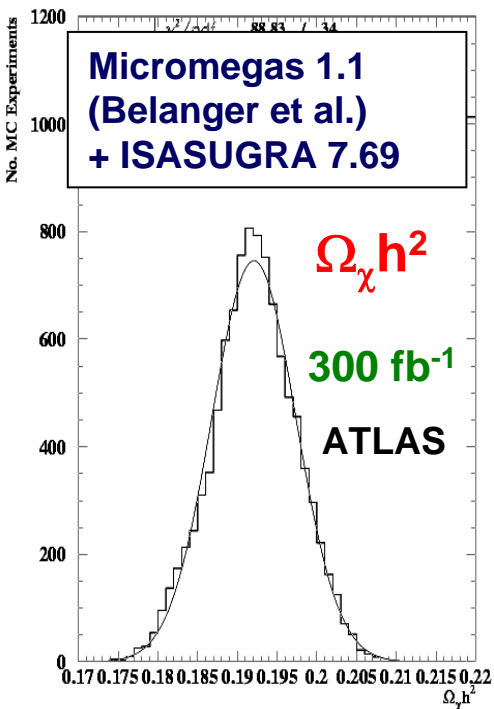




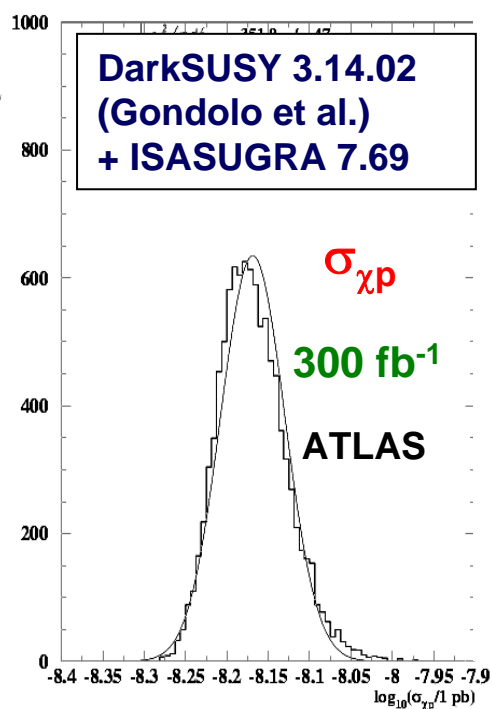
SUSY Dark Matter



- Can use parameter measurements for many purposes, e.g. estimate LSP Dark Matter properties (e.g. for 300 fb⁻¹, SPS1a)
 - $\Omega_\chi h^2 = 0.1921 \pm 0.0053$
 - $\log_{10}(\sigma_{\chi p}/\text{pb}) = -8.17 \pm 0.04$



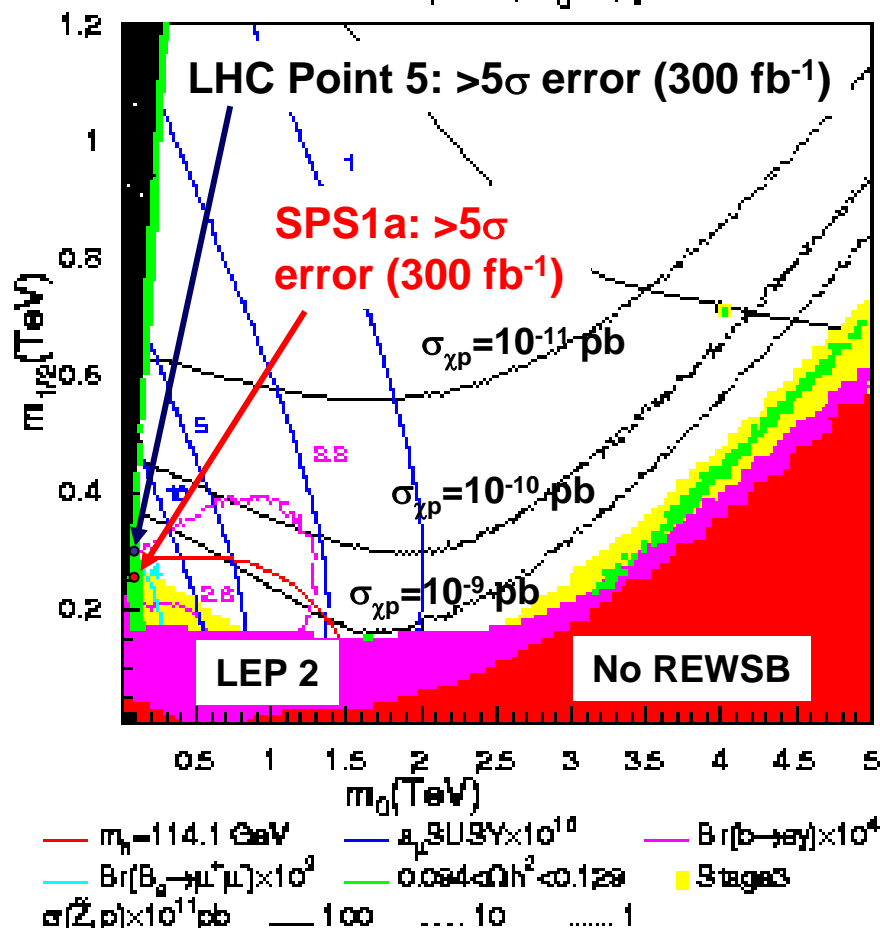
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Baer et al. hep-ph/0305191

mSUGRA, tan $\beta=10, A_0=0, \mu>0$



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SUSY Dark Matter

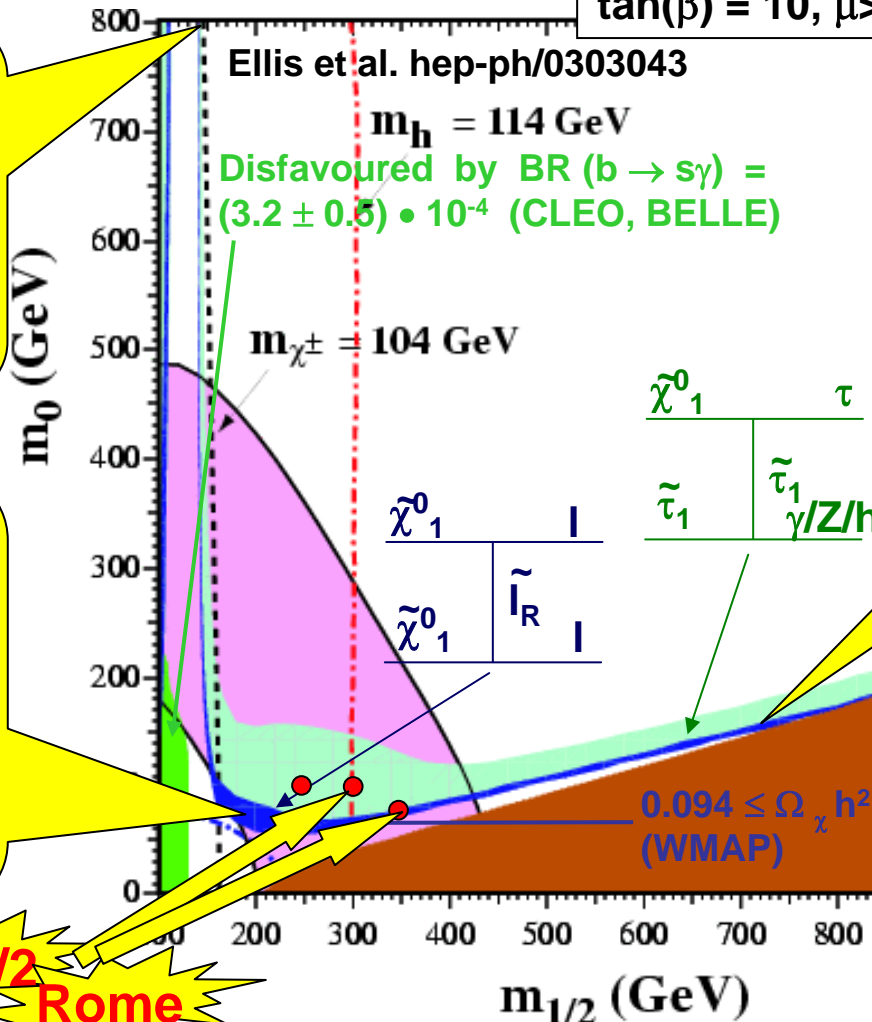
- SUSY (e.g. mSUGRA) parameter space strongly constrained by cosmology (e.g. WMAP satellite) data.

mSUGRA $A_0=0$,
 $\tan(\beta) = 10$, $\mu > 0$

'Focus point' region: significant \tilde{n} component to LSP enhances annihilation to gauge bosons

'Bulk' region: t-channel slepton exchange - LSP mostly Bino.
'Bread and Butter' region for LHC Expts.

Slepton Co-annihilation region: LSP ~ pure Bino. Small slepton-LSP mass difference makes measurements difficult.

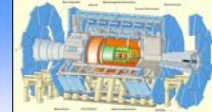


Also 'rapid annihilation funnel' at Higgs pole at high $\tan(\beta)$, stop co-annihilation region at large A_0

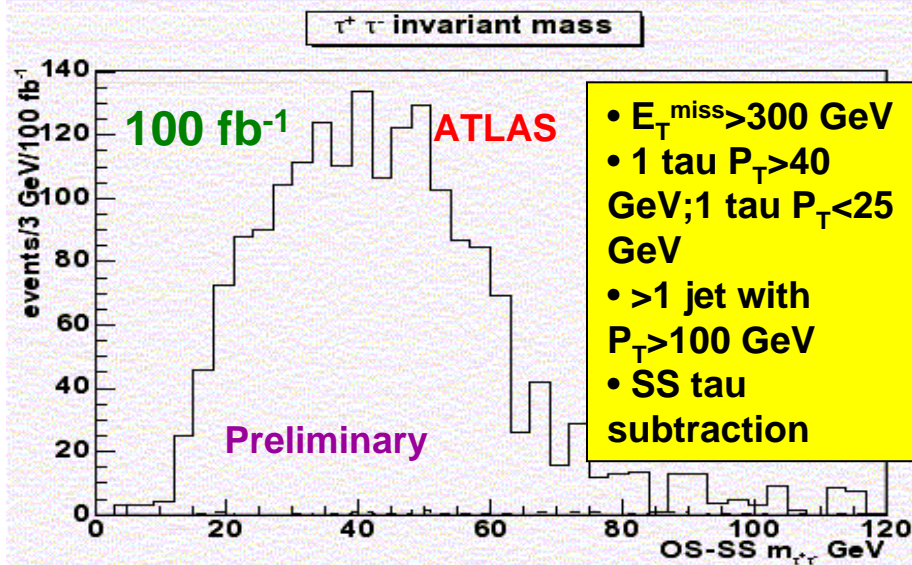
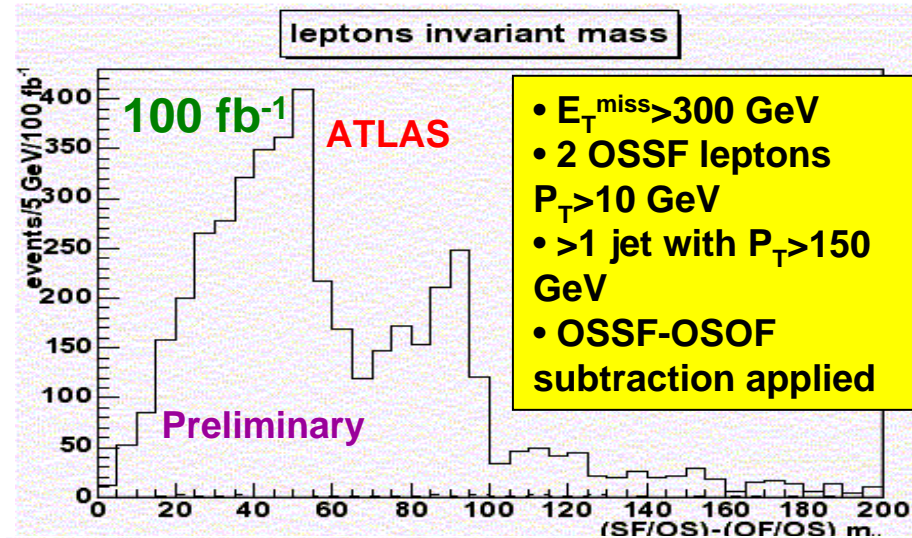
DC1/2
Rome



Coannihilation Signatures



- **Small slepton-neutralino mass difference gives soft leptons**
 - Low electron/muon/tau energy thresholds crucial.
- **Study point chosen within region:**
 - $m_0=70$ GeV; $m_{1/2}=350$ GeV; $A_0=0$; $\tan\beta=10$; $\mu > 0$;
 - Same model used for DC2 study.
- **Decays of $\tilde{\chi}_2^0$ to both \tilde{L}_L and \tilde{L}_R kinematically allowed.**
 - Double dilepton invariant mass edge structure;
 - Edges expected at 57 / 101 GeV
- **Stau channels enhanced ($\tan\beta$)**
 - Soft tau signatures;
 - Edge expected at 79 GeV;
 - Less clear due to poor tau visible energy resolution.

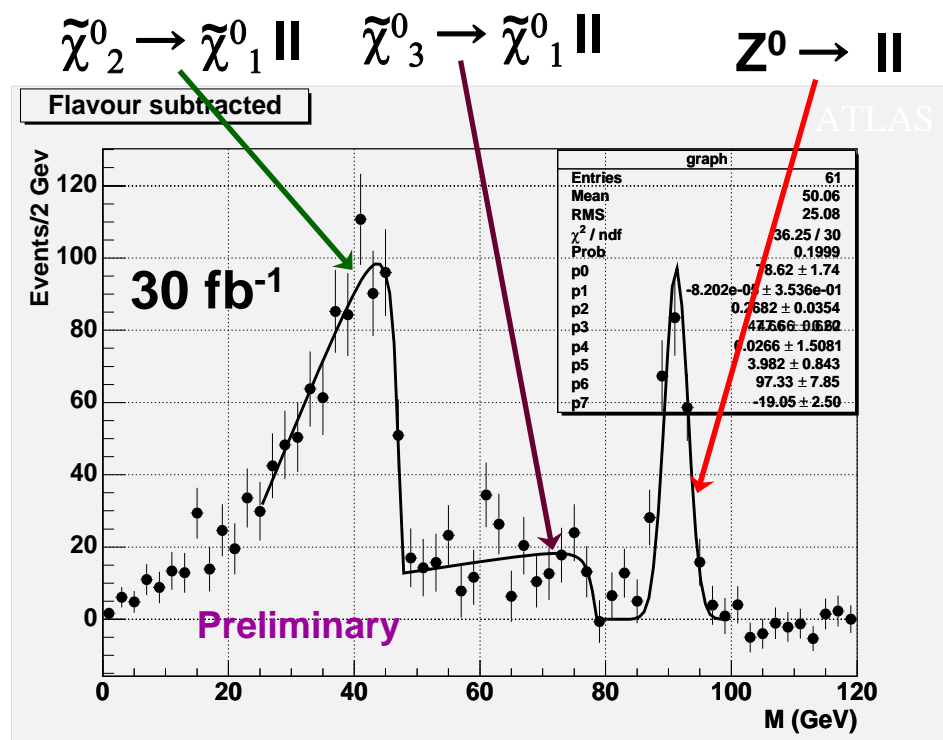
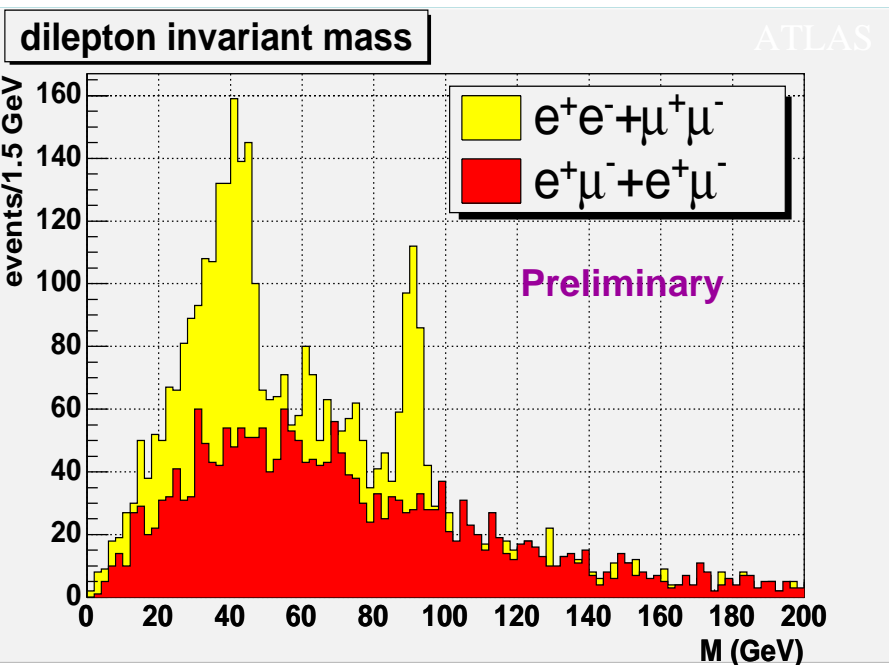


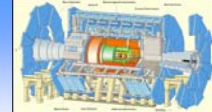


Focus Point Models



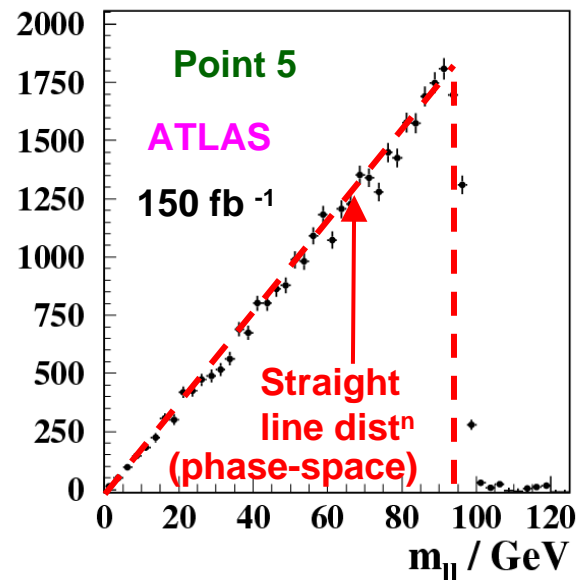
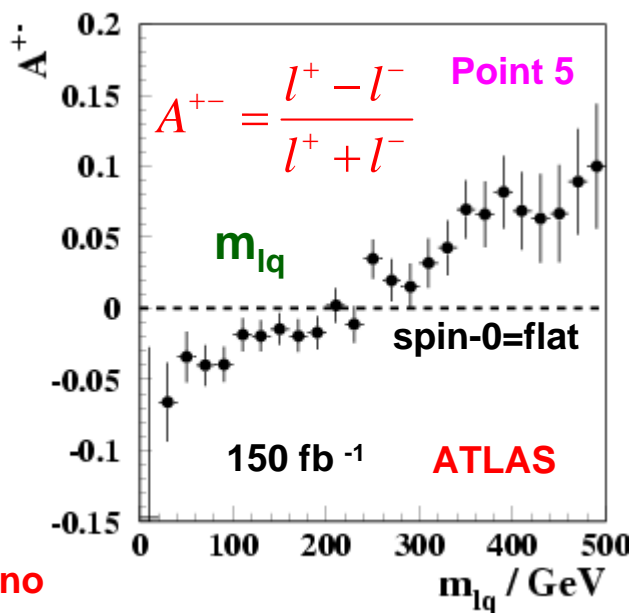
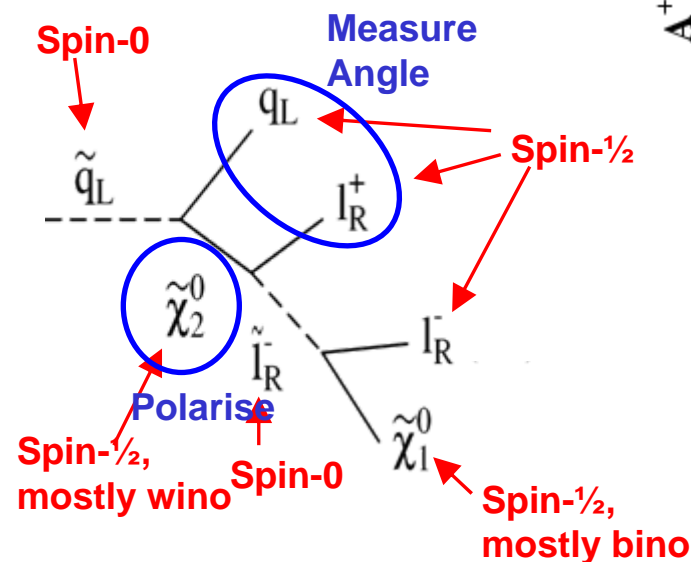
- Large $m_0 \rightarrow$ sfermions are heavy
- Most useful signatures from heavy neutralino decay
- Study point chosen within focus point region :
 - $m_0=3000$ GeV; $m_{1/2}=215$ GeV; $A_0=0$; $\tan\beta=10$; $\mu > 0$
- Direct three-body decays $\tilde{\chi}^0_n \rightarrow \tilde{\chi}^0_1 \parallel$
- Edges give $m(\tilde{\chi}^0_n)-m(\tilde{\chi}^0_1)$





SUSY Spin Measurement

- **Q: How do we know that a SUSY signal is really due to SUSY?**
 - Other models (e.g. UED) can mimic SUSY mass spectrum
- **A: Measure spin of new particles.**
- **One proposal – use ‘standard’ two-body slepton decay chain**
 - charge asymmetry of lq pairs measures spin of $\tilde{\chi}_2^0$
 - relies on valence quark contribution to pdf of proton (C asymmetry)
 - shape of dilepton invariant mass spectrum measures slepton spin

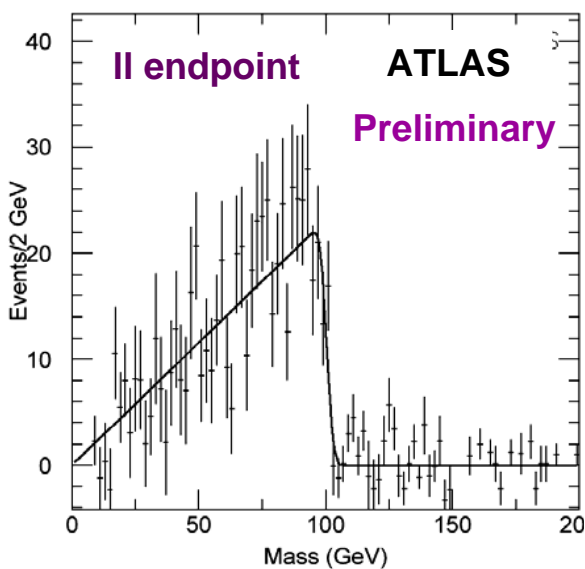
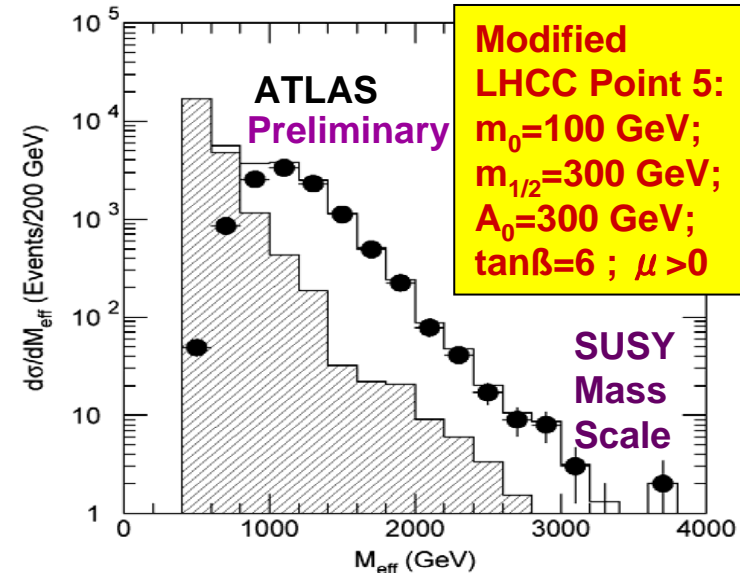




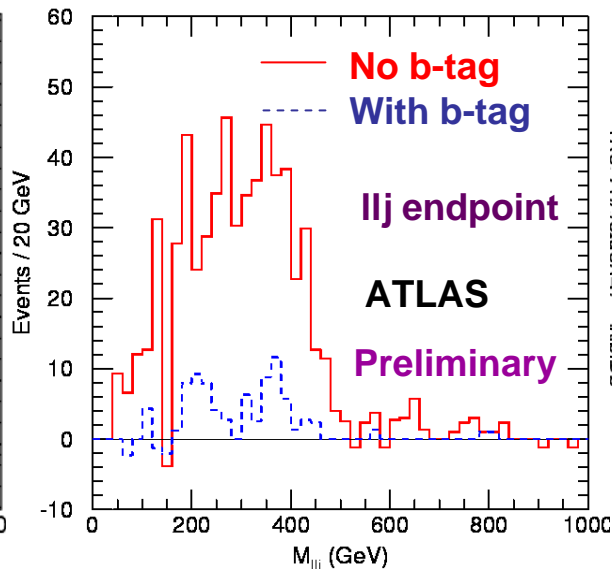
DC1 SUSY Challenge



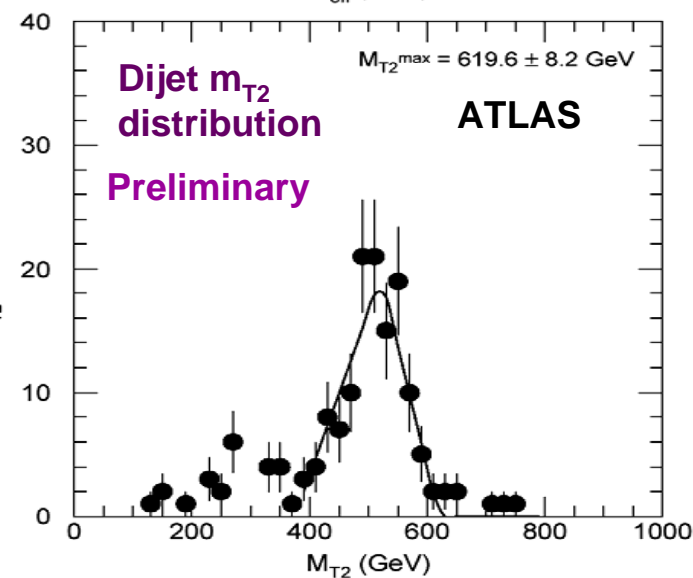
- First attempt at large-scale simulation of SUSY signals in ATLAS (100 000 events: $\sim 5 \text{ fb}^{-1}$) in early 2003.
- Tested Geant3 simulation and ATHENA (C++) reconstruction software framework thoroughly.



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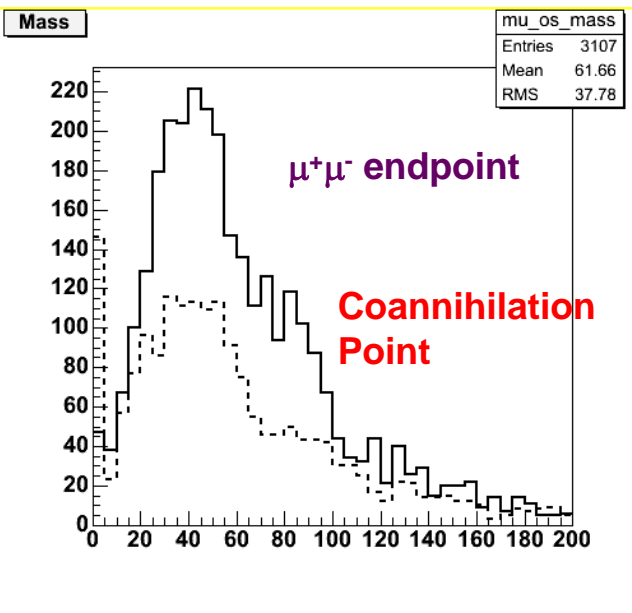
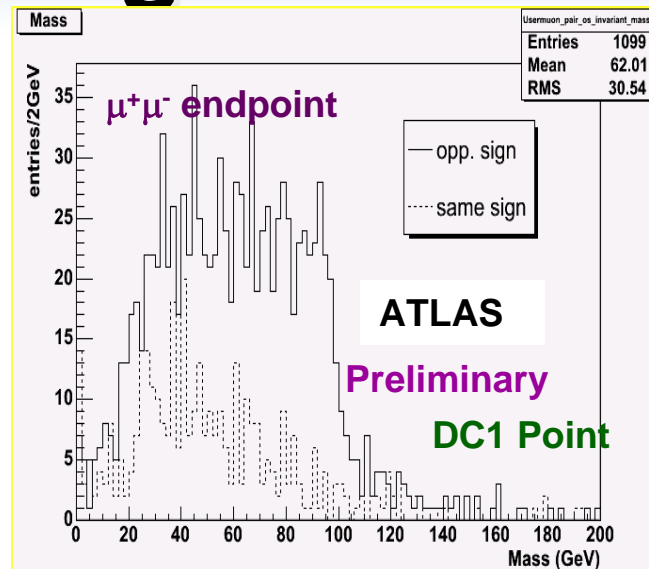
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DC2 SUSY Challenge

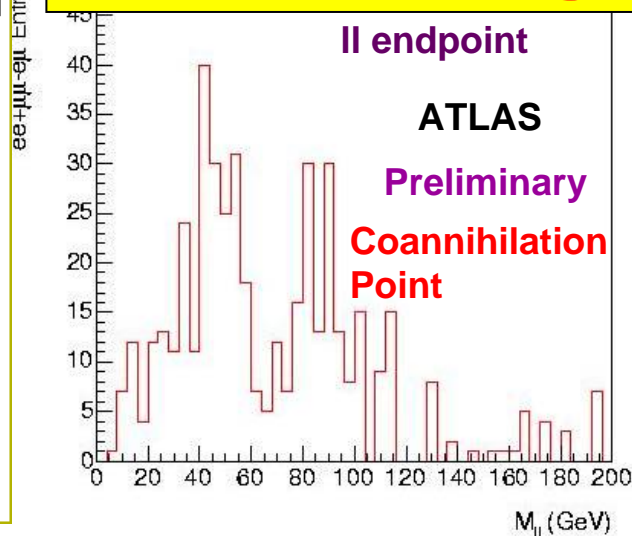


- DC2 testing new G4 simulation and reconstruction.
- Points studied:
 - DC1 bulk region point (test G4)
 - Stau coannihilation point (rich in signatures - test reconstruction)
- Further studies planned in run up to Rome Physics Workshop (Focus Point model etc.)

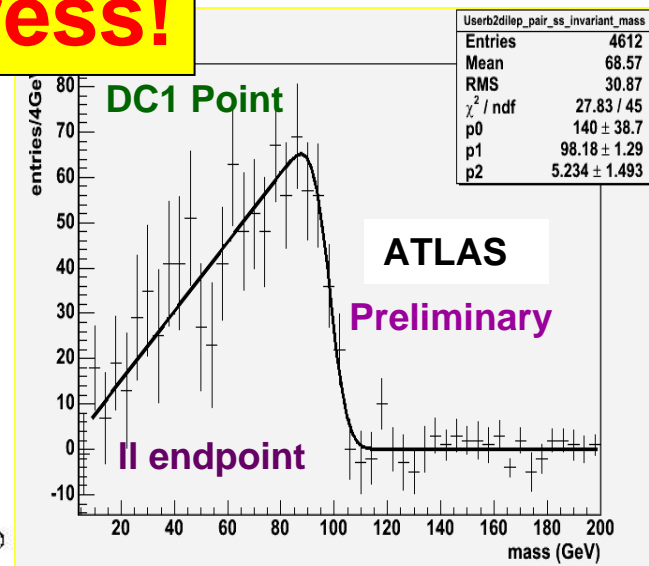


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Work in Progress!



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Preparations for 1st Physics

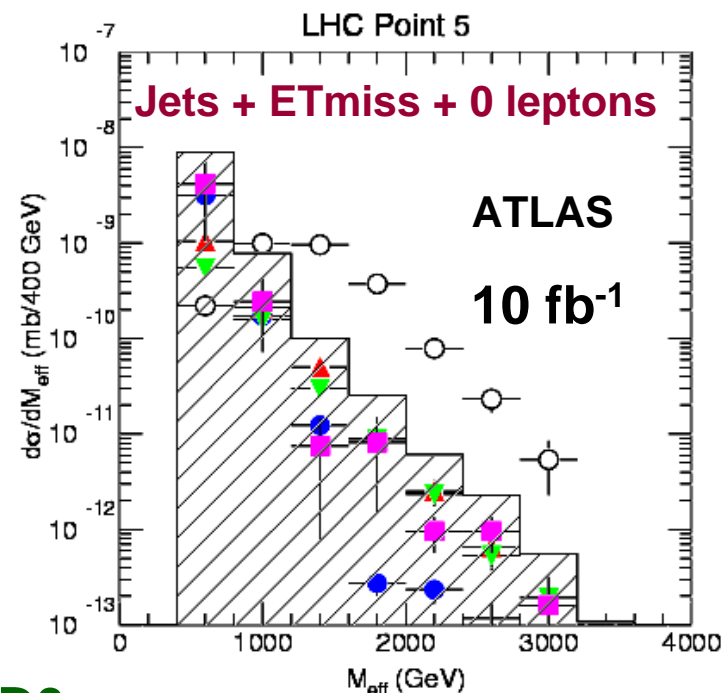


- Preparations needed to ensure efficient/reliable searches for/measurements of SUSY particles in timely manner:
 - Initial calibrations (energy scales, resolutions, efficiencies etc.);
 - Minimisation of poorly estimated SM backgrounds;
 - Estimation of remaining SM backgrounds;
 - Development of useful tools.
- Different situation to Run II (no previous σ measurements at same \sqrt{s})
- Will need convincing bckgrnd. estimate with little data as possible.
- Background estimation techniques will change depending on integrated lumi.
- Ditto optimum search channels & cuts.
- Aim to use combination of
 - Fast-sim;
 - Full-sim;
 - Estimations from data.
- Use comparison between different techniques to validate estimates and build confidence in (blind) analysis.
- Aim to study with full-sim (DC2) data

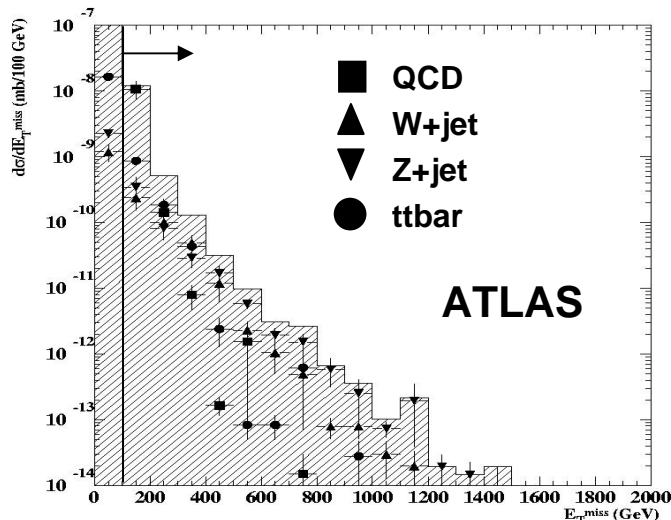


Background Estimation

- **Main backgrounds:**
 - Z + n jets
 - W + n jets
 - ttbar
 - QCD
- **Generic approach :**
 - Select low E_T^{miss} background calibration samples;
 - Extrapolate into high E_T^{miss} signal region.
- **Also:**
 - Single top
 - WW/WZ/ZZ



- Used by CDF / D0
- Extrapolation non-trivial.
 - Must find variables uncorrelated with E_T^{miss}
- Several approaches developed.
- Most promising: Use Z ($\rightarrow \ell\ell$) + jets to estimate Z ($\rightarrow \nu\nu$) / W ($\rightarrow \ell\nu$) + jets

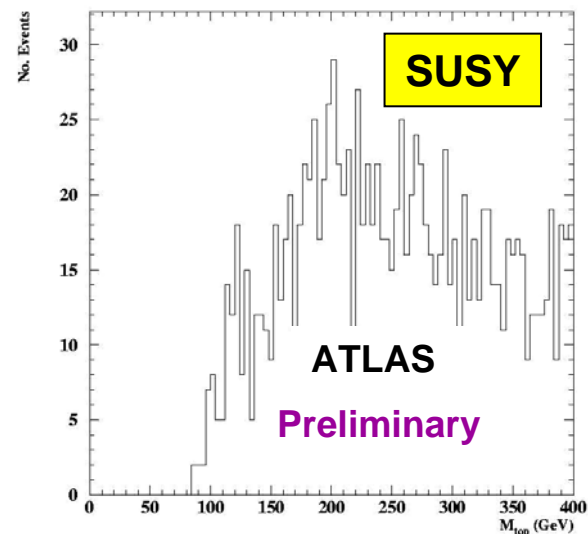
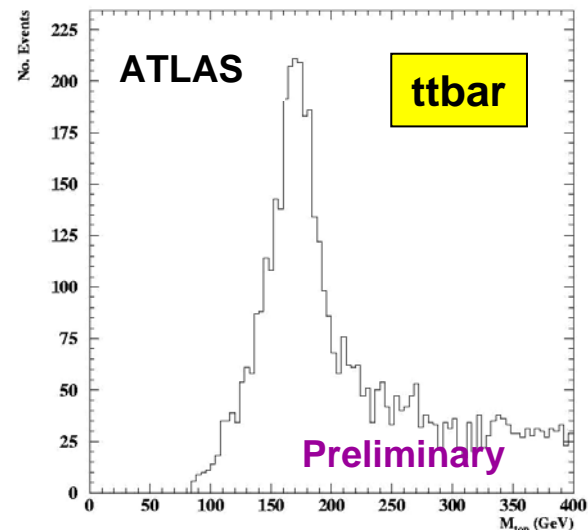




Top Background



- Estimation using simulation possible (normalised to data $t\bar{t}$ selection) – cross-check with data
- Isolate clean sample of top events using mass constraint(s).
- Then plot E_T^{miss} distribution (large statistical errors), compare with same technique applied to SUSY events (SPS1a benchmark model).
- Reconstruct leptonic W momentum from E_T^{miss} vector and W mass constraint (analytical approach – quadratic ambiguity).
- Select solution with greatest W p_T .
- Select b -jet with greatest p_T .
- Plot invariant mass of combination.

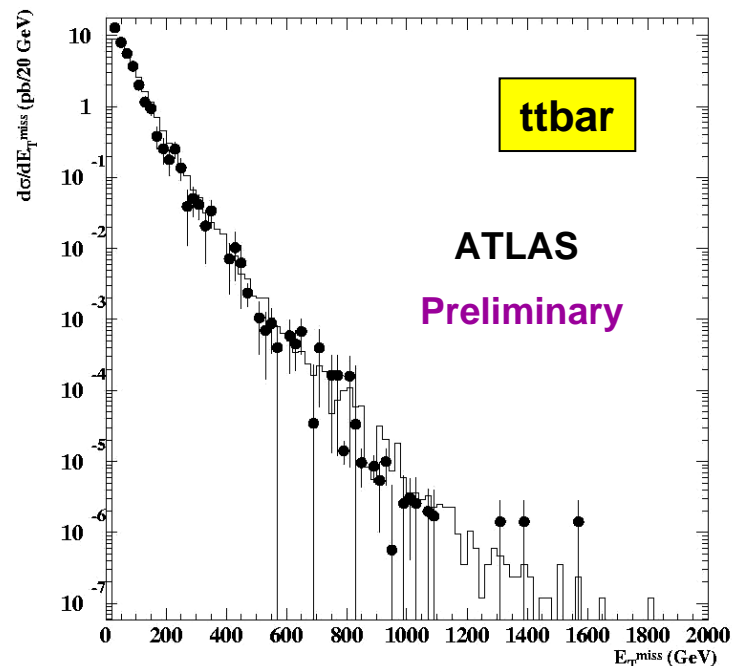
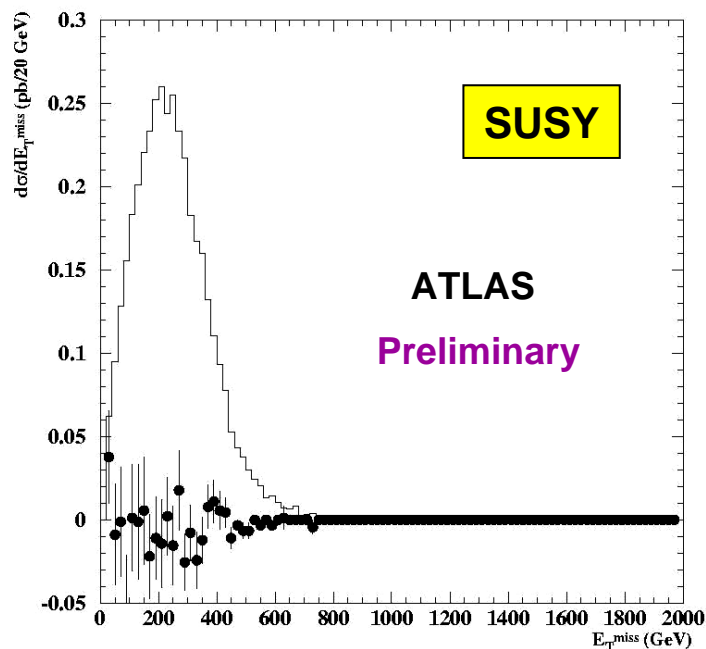




Top Background



- Select events in peak and examine $E_{T,miss}$ distribution.
- Subtract combinatorial background with appropriately weighted (from MC) sideband subtraction.
- Good agreement with top background distribution in SUSY selection.



- With this tuning does not select SUSY events (as required)
- Promising approach but more work needed (no btag etc.)

Histogram – 1 lepton SUSY selection (no b-tag)
Data points – background estimate



Supersummary

- The LHC will be THE PLACE to search for, and hopefully study, SUSY from 2007 onwards (at least until ILC).
- SUSY searches will commence on Day 1 of LHC operation.
- Many studies of exclusive channels already performed.
- Lots of input from both theorists (new ideas) and experimentalists (new techniques).
- Renewed emphasis on use of full simulation tools.
- Big challenge for discovery will be understanding systematics.
- Big effort ramping up now to understand how to exploit first data in timely fashion
 - Calibrations
 - Background rejection
 - Background estimation
 - Tools
- Massive scope for further work!

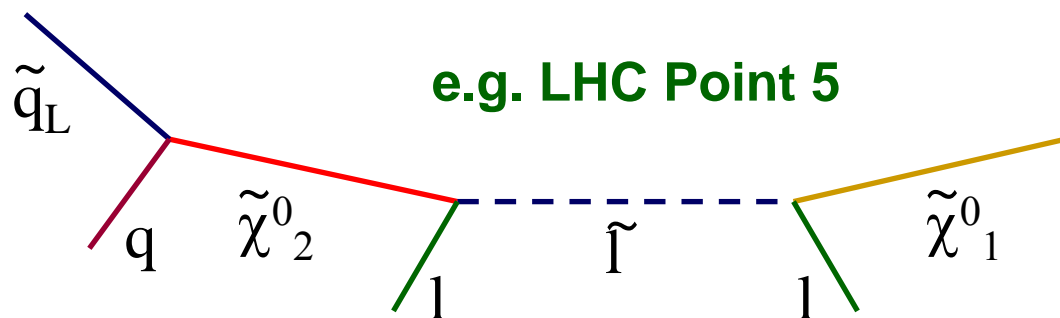


BACK-UP SLIDES



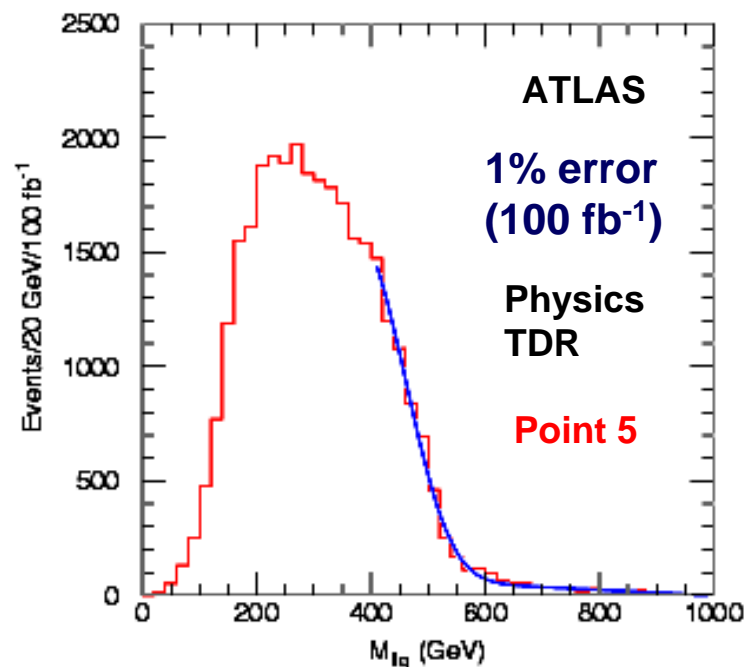
llq Edge

- Dilepton edges provide starting point for other measurements.
- Use dilepton signature to tag presence of $\tilde{\chi}^0_2$ in event, then work back up decay chain constructing invariant mass distributions of combinations of leptons and jets.



$$M_{llq}^{\max} = \left[\frac{(M_{q_L}^2 - M_{\tilde{\chi}_2^0}^2)(M_{\tilde{\chi}_2^0}^2 - M_{\tilde{\chi}_1^0}^2)}{M_{\tilde{\chi}_2^0}^2} \right]^{1/2} = 552.4 \text{ GeV}.$$

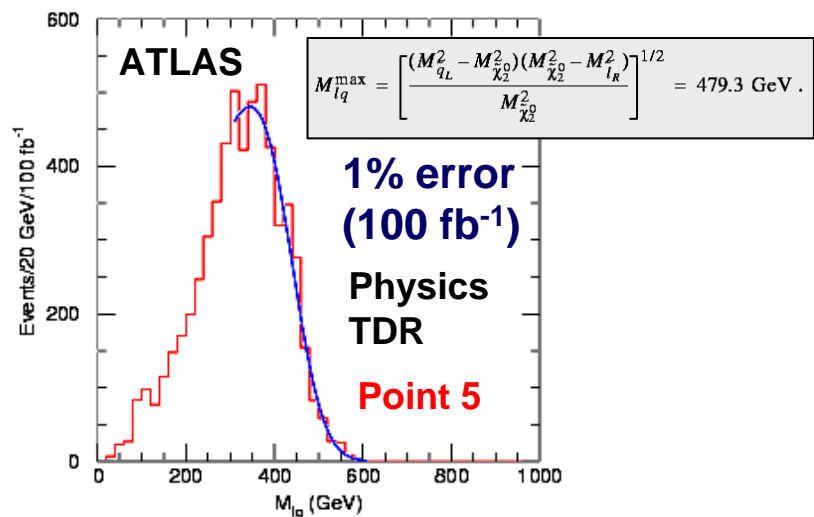
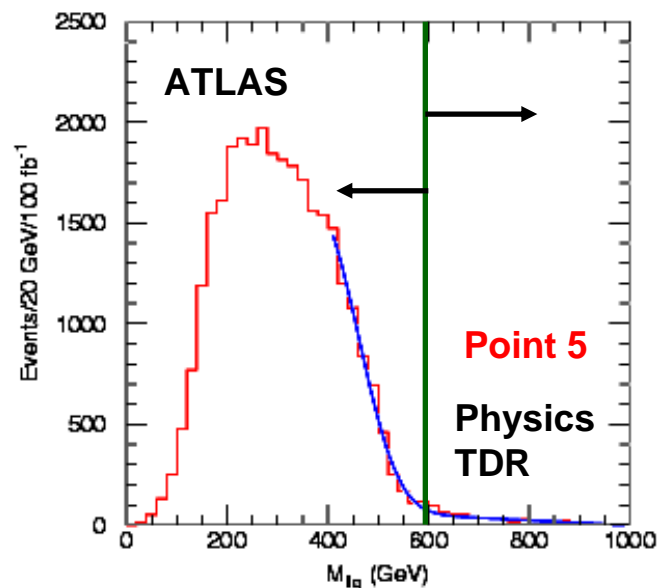
- Hardest jets in each event produced by RH or LH squark decays.
- Select smaller of two llq invariant masses from two hardest jets
 - Mass must be $<$ edge position.
- Edge sensitive to LH squark mass.



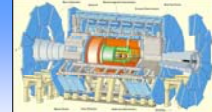


Iq Edge

- Complex decay chain at LHC Point 5 gives additional constraints on masses.
- Use lepton-jet combinations in addition to lepton-lepton combinations.
- Select events with only one dilepton-jet pairing consistent with slepton hypothesis
 - Require one lq mass above edge and one below (reduces combinatorics).

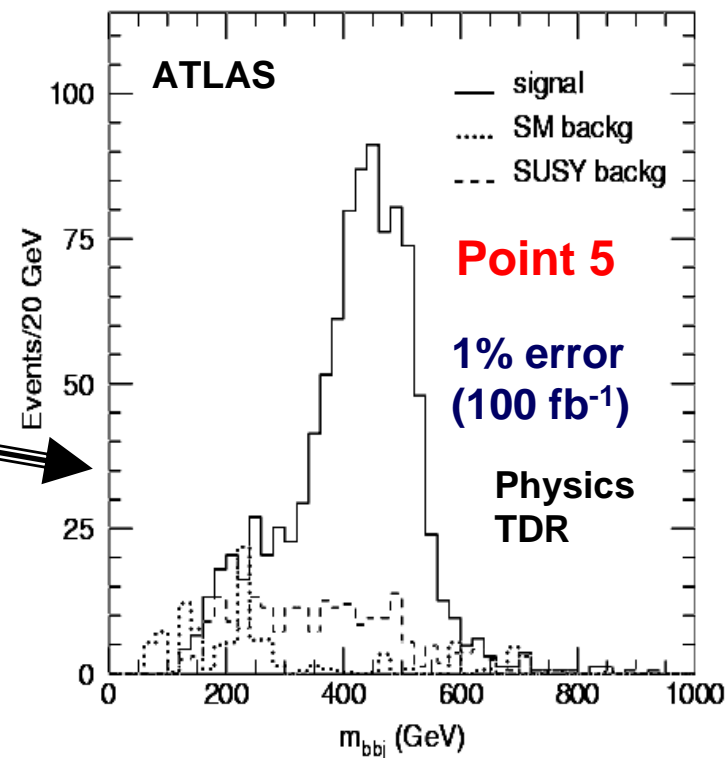
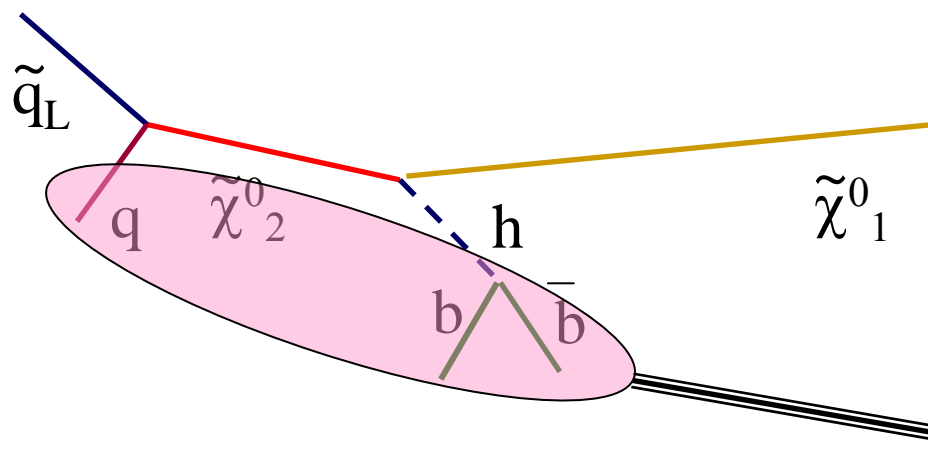


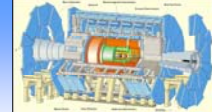
- Construct distribution of invariant masses of 'slepton' jet with each lepton.
- 'Right' edge sensitive to slepton, squark and $\tilde{\chi}_2^0$ masses ('wrong' edge not visible).



hq edge

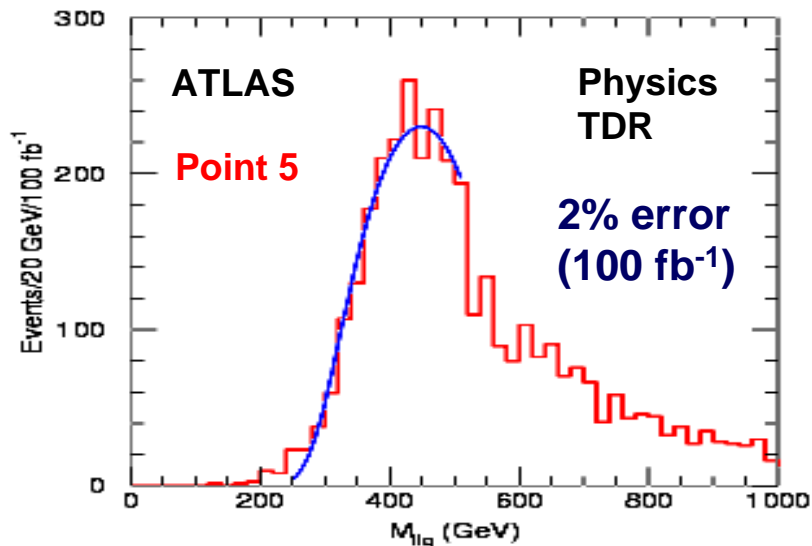
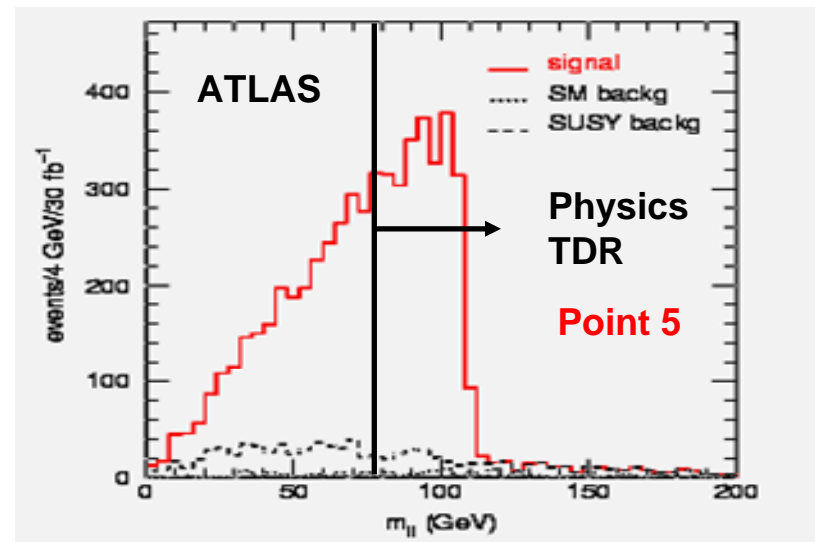
- If $\tan(\beta)$ not too large can also observe two body decay of $\tilde{\chi}^0_2$ to higgs and $\tilde{\chi}^0_1$.
- Reconstruct higgs mass (2 b-jets) and combine with hard jet.
- Gives additional mass constraint.





llq Threshold

- Two body kinematics of slepton-mediated decay chain also provides still further information (Point 5).
- Consider case where $\tilde{\chi}^0_1$ produced near rest in $\tilde{\chi}^0_2$ frame.
 - ➔ Dilepton mass near maximal.
 - ➔ $p(l\bar{l})$ determined by $p(\tilde{\chi}^0_2)$.



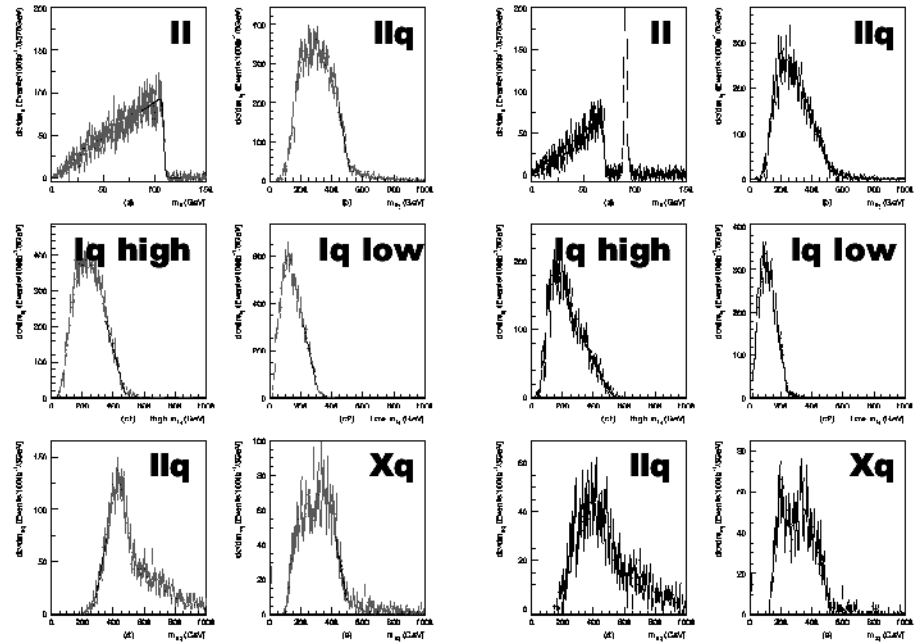
- Distribution of llq invariant masses distribution has maximum and minimum (when quark and dilepton parallel).
- llq threshold important as contains new dependence on mass of lightest neutralino.



Mass Reconstruction



- Combine measurements from edges from different jet/lepton combinations.



- Gives sensitivity to masses (rather than combinations).

Related edge	Kinematic endpoint
l^+l^- edge	$\langle m_{ll}^{\max} \rangle^2 = (\xi - \tilde{l})(\tilde{l} - \bar{\chi})/\tilde{l}$
l^+l^-q edge	$\langle m_{llq}^{\max} \rangle^2 = \begin{cases} \max \left[(\tilde{q} - \xi)(\xi - \bar{\chi}), (\tilde{q} - \tilde{l})(\tilde{l} - \bar{\chi}), (\tilde{q} - \xi)\tilde{l}(\xi - \tilde{l}) \right] \\ \text{except for the special case in which } \tilde{l}^2 < \tilde{q}\bar{\chi} < \xi^2 \text{ and} \\ \xi^2\bar{\chi} < \tilde{q}\tilde{l}^2 \text{ where one must use } (m_{\tilde{q}} - m_{\tilde{\chi}_2^0})^2. \end{cases}$
Xq edge	$\langle m_{Xq}^{\max} \rangle^2 = X + (\tilde{q} - \xi) \left[\xi + X - \bar{\chi} + \sqrt{(\xi - X - \bar{\chi})^2 - 4X\bar{\chi}} \right] / (2\xi)$
l^+l^-q threshold	$\langle m_{llq}^{\min} \rangle^2 = \begin{cases} [2\tilde{l}(\tilde{q} - \xi)(\xi - \bar{\chi}) + (\tilde{q} + \xi)(\xi - \tilde{l})(\tilde{l} - \bar{\chi}) \\ -(\tilde{q} - \xi)\sqrt{(\xi + \tilde{l})^2(\tilde{l} + \bar{\chi})^2 - 16\xi\tilde{l}^2\bar{\chi}}] / (4\xi\tilde{l}) \end{cases}$
$l_{near}^\perp q$ edge	$\langle m_{l_{near}^\perp q}^{\max} \rangle^2 = (\tilde{q} - \xi)(\xi - \tilde{l})/\xi$
$l_{far}^\pm q$ edge	$\langle m_{l_{far}^\pm q}^{\max} \rangle^2 = (\tilde{q} - \xi)(\tilde{l} - \bar{\chi})/\tilde{l}$
$l^\pm q$ high-edge	$\langle m_{lq}^{\max} \rangle^2 = \max \left[\langle m_{l_{near}^\perp q}^{\max} \rangle^2, \langle m_{l_{far}^\pm q}^{\max} \rangle^2 \right]$
$l^\pm q$ low-edge	$\langle m_{lq}^{\max} \rangle^2 = \min \left[\langle m_{l_{near}^\perp q}^{\max} \rangle^2, \langle m_{l_{far}^\pm q}^{\max} \rangle^2 \right]$
M_{T2} edge	$\Delta M = m_{\tilde{q}} - m_{\tilde{\chi}_2^0}$

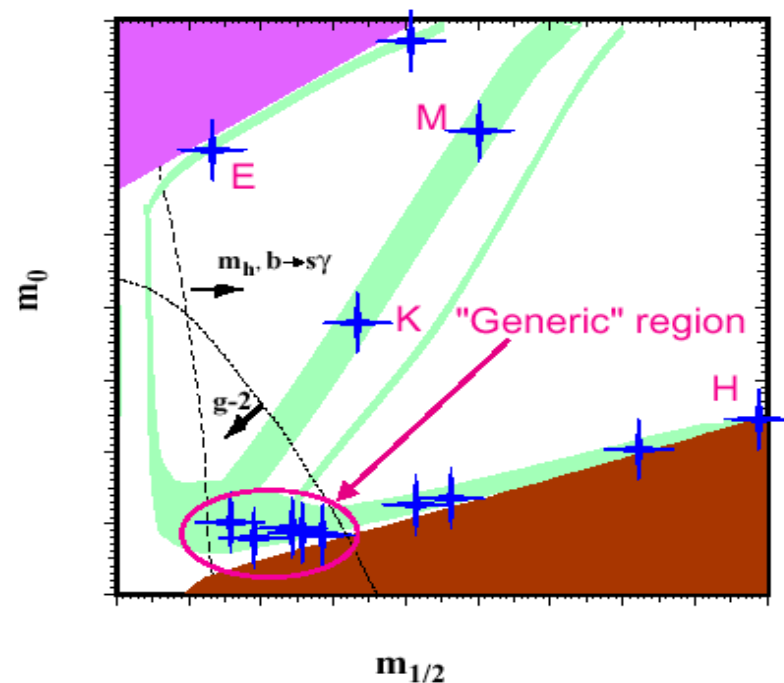
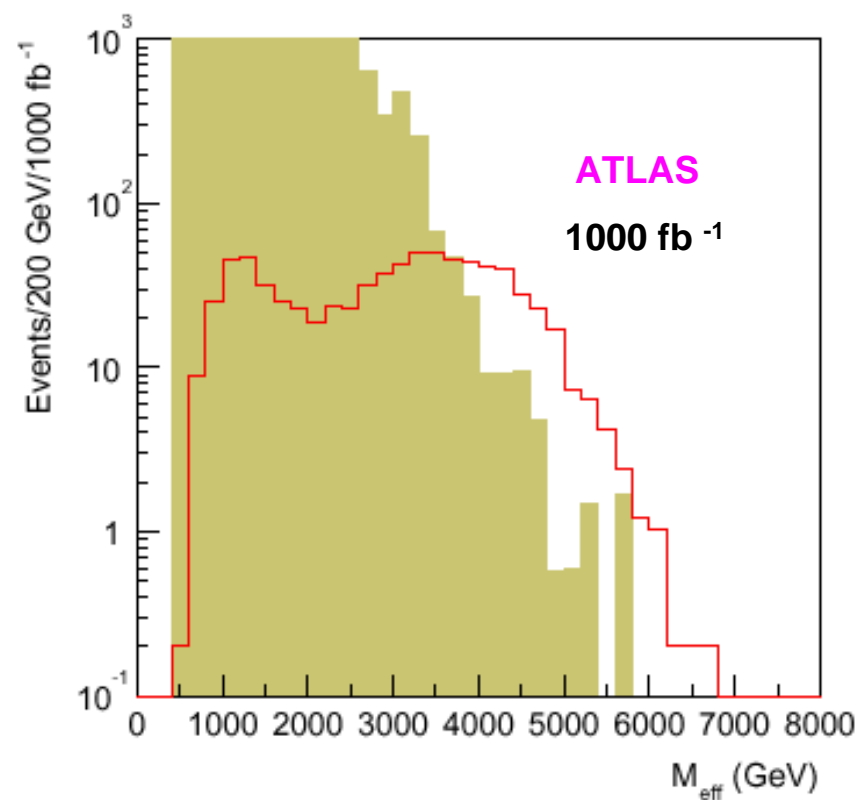
Table 4: The absolute kinematic endpoints of invariant mass quantities formed from decay chains of the types mentioned in the text for known particle masses. The following shorthand notation has been used: $\bar{\chi} = m_{\tilde{\chi}_1^0}$, $\tilde{l} = m_{\tilde{l}}$, $\xi = m_{\tilde{\chi}_2^0}$, $\tilde{q} = m_{\tilde{q}}$ and X is m_X^2 or $m_{\tilde{g}}^2$ depending on which particle participates in the "branched" decay.



High Mass mSUGRA



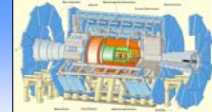
- ATLAS study of sensitivity to models with high mass scales
- E.g. CLIC Point K → Potentially observable ... but hard!



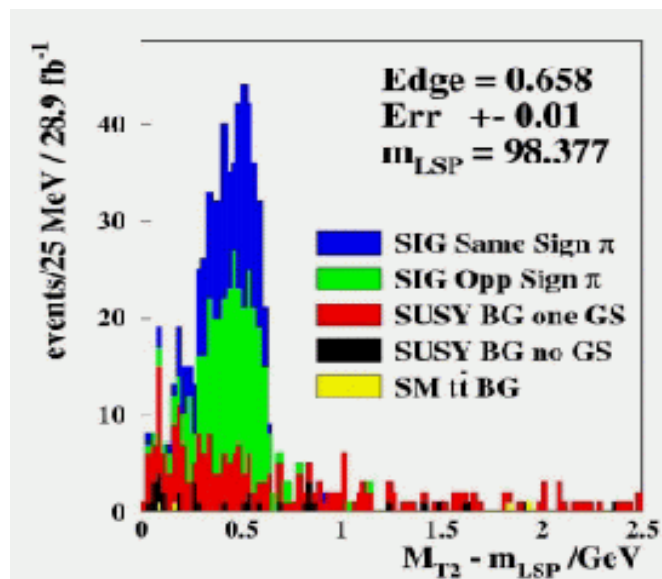
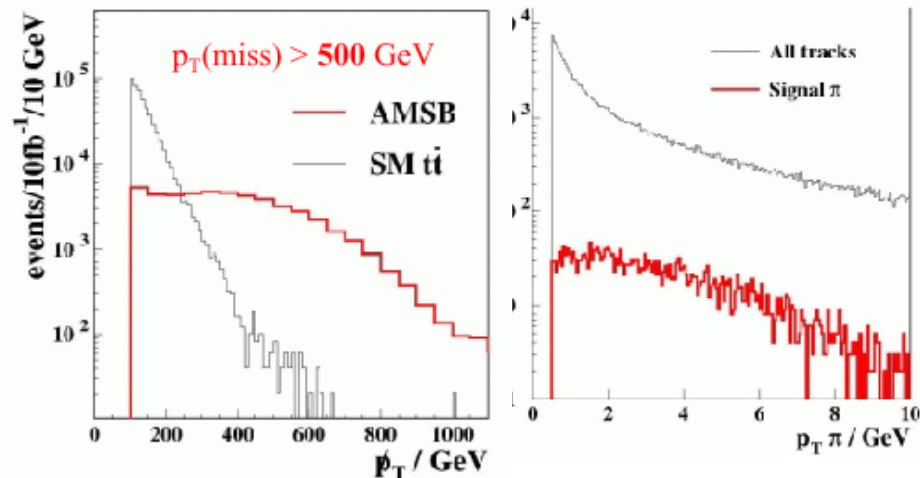
- Characteristic double peak in signal M_{eff} distribution (Point K).
- Squark and gluino production cross-section reduced due to high mass.
- Gaugino production significant



AMSB



- Examined RPC model with $\tan(\beta) = 10$, $m_{3/2}=36$ TeV, $m_0=500$ GeV, $\text{sign}(\mu) = +1$.
- $\tilde{\chi}^{\pm 1}_1$ near degenerate with $\tilde{\chi}^0_1$.
- Search for $\tilde{\chi}^{\pm 1}_1 \rightarrow \pi^{\pm} \tilde{\chi}^0_1$ ($\Delta m = 631$ MeV \rightarrow soft pions).



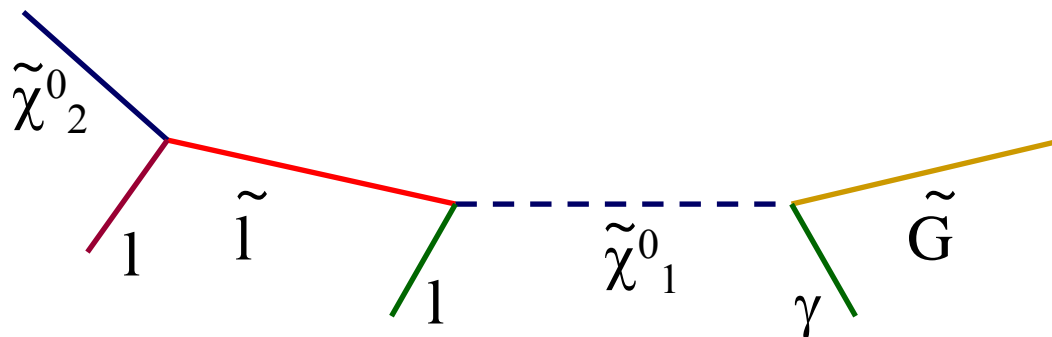
- Also displaced vertex due to phase space ($c\tau=360$ microns).
- Measure mass difference between chargino and neutralino using m_{T2} variable (from mSUGRA analysis).



GMSB

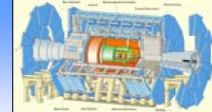


- Kinematic edges also useful for GMSB models when neutral LSP or very long-lived NLSP escapes detector.
- Kinematic techniques using invariant masses of combinations of leptons, jets and photons similar.
- Interpretation different though.
- E.g. LHC Point G1a (neutralino NLSP with prompt decay to gravitino) with decay chain:

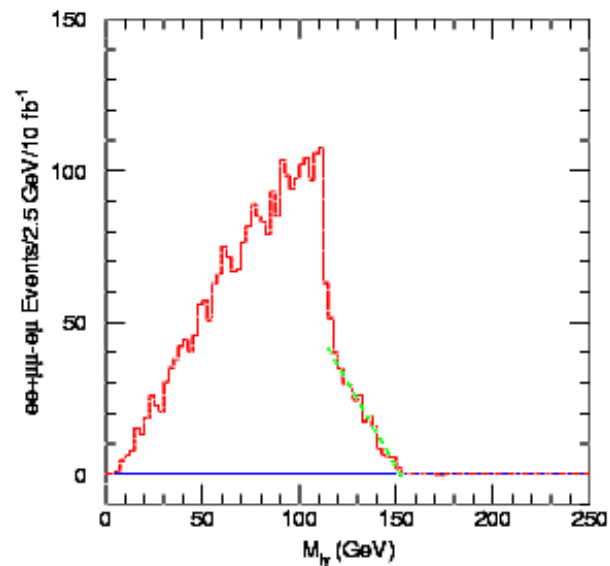
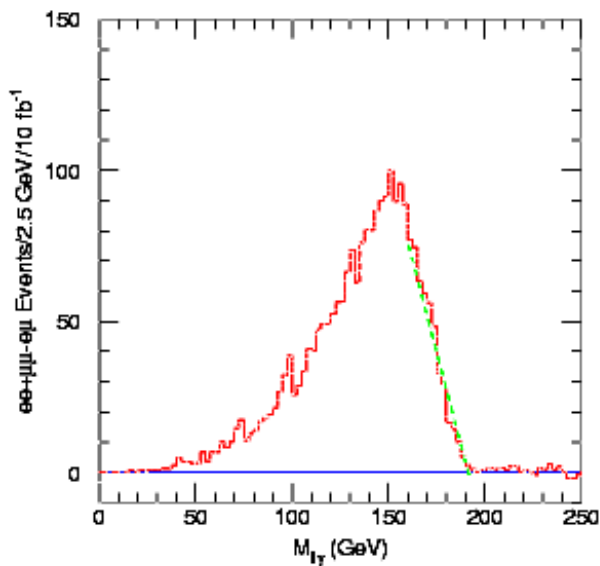
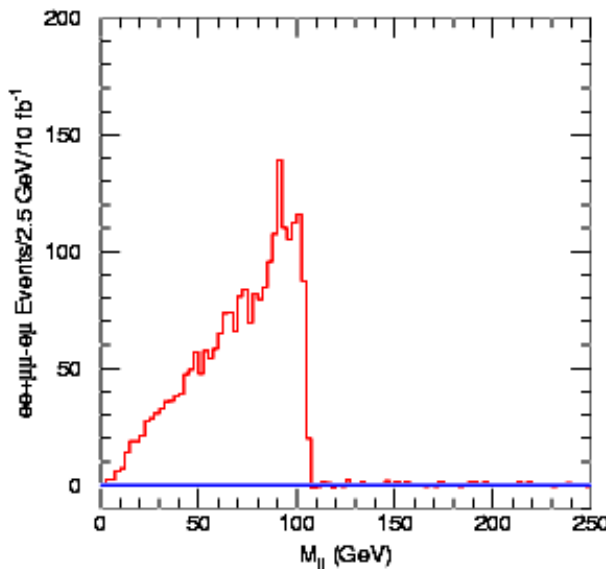




GMSB



- Use dilepton edge as before (but different position in chain).
- Use also $l\gamma$, $ll\gamma$ edges (c.f. lq and llq edges in mSUGRA).
- Get two edges (bonus!) in $l\gamma$ as can now see edge from 'wrong' lepton (from χ^0_2 decay). Not possible at LHCC Pt5 due to masses.

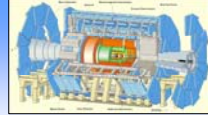


- Interpretation easier as can assume gravitino massless:

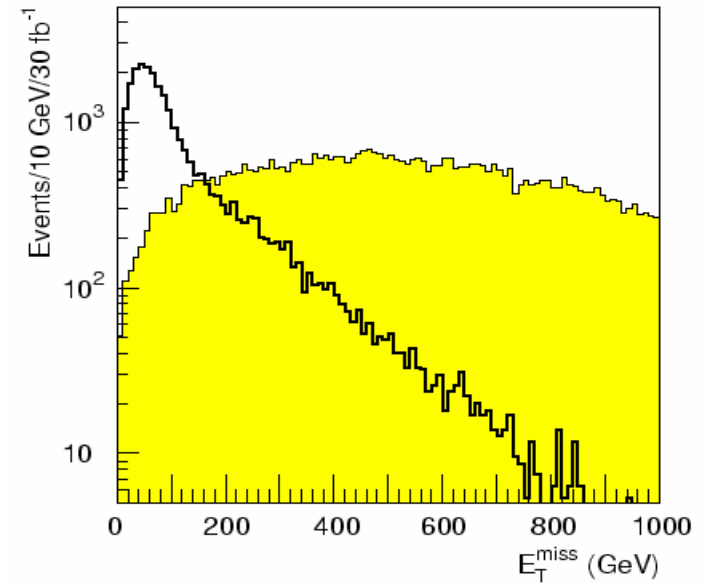
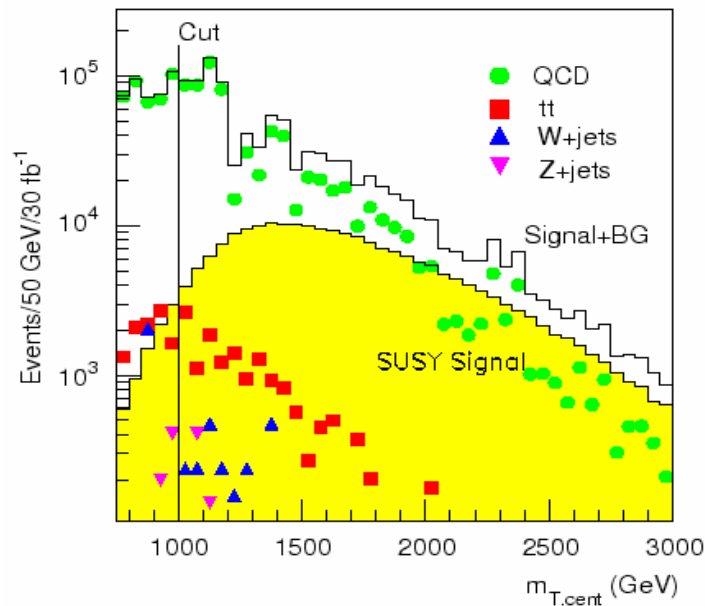
$$M_{l_R}^2 = \frac{(M_{l\gamma}^{(1)})^2 (M_{l\gamma}^{(2)})^2}{(M_{ll}^{\max})^2} \quad M_{\chi_1^0}^2 = M_{l_R}^2 - (M_{l\gamma}^{(1)})^2 \quad M_{\chi_2^0}^2 = M_{l_R}^2 + (M_{l\gamma}^{(2)})^2 \quad (M_{ll\gamma}^{\max})^2 = (M_{l\gamma}^{(1)})^2 + (M_{l\gamma}^{(2)})^2.$$



R-Parity Violation



- Missing E_T for events at SUGRA point 5 with and without R-parity violation
- RPV removes the classic SUSY missing E_T signature



- Use modified effective mass variable taking into account p_T of leptons and jets in event

$$m_{T,cent} = \sum_{\eta < 2} p_T^{jet, lepton}$$



R-Parity Violation



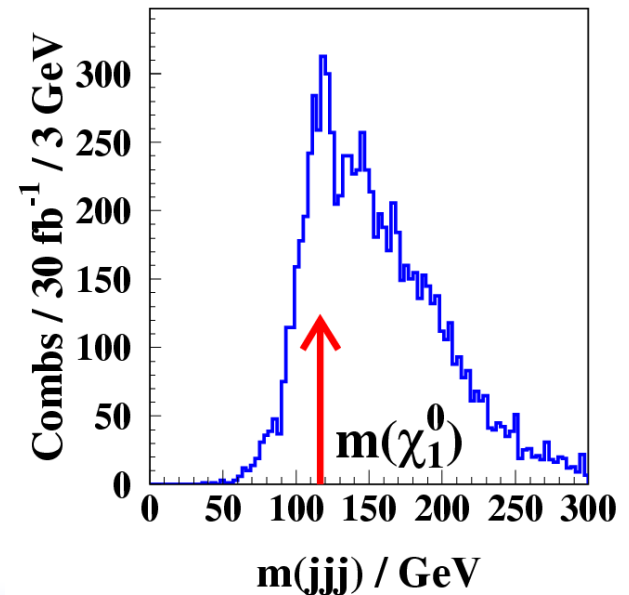
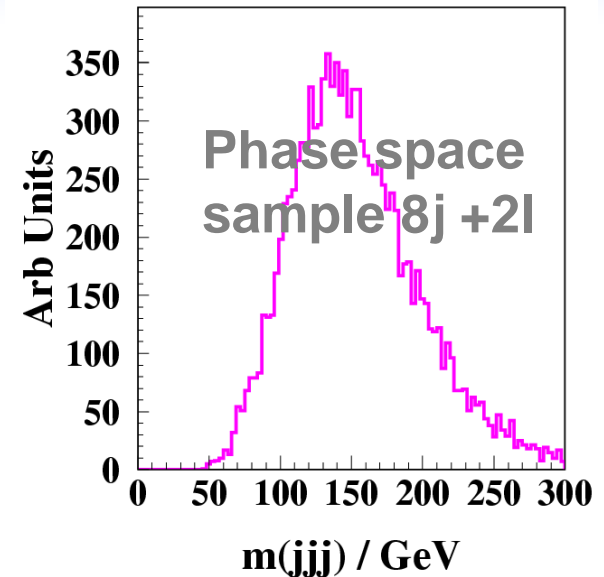
- **Baryon-Parity violating case hardest to identify (no leptons).**
 - **Worst case: λ''_{212} - no heavy-quark jets**
- **Test model studied with decay chain:**

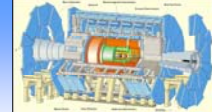
$$\tilde{q}_L \rightarrow \tilde{\chi}_2^0 q \rightarrow \tilde{l}_R l q \rightarrow \tilde{\chi}_1^0 l l q$$

- **Lightest neutralino decays via BPV coupling:**

$$\tilde{\chi}_1^0 \rightarrow cds$$

- **Reconstruct neutralino mass from 3-jet combinations (but large combinatorics : require > 8 jets!)**

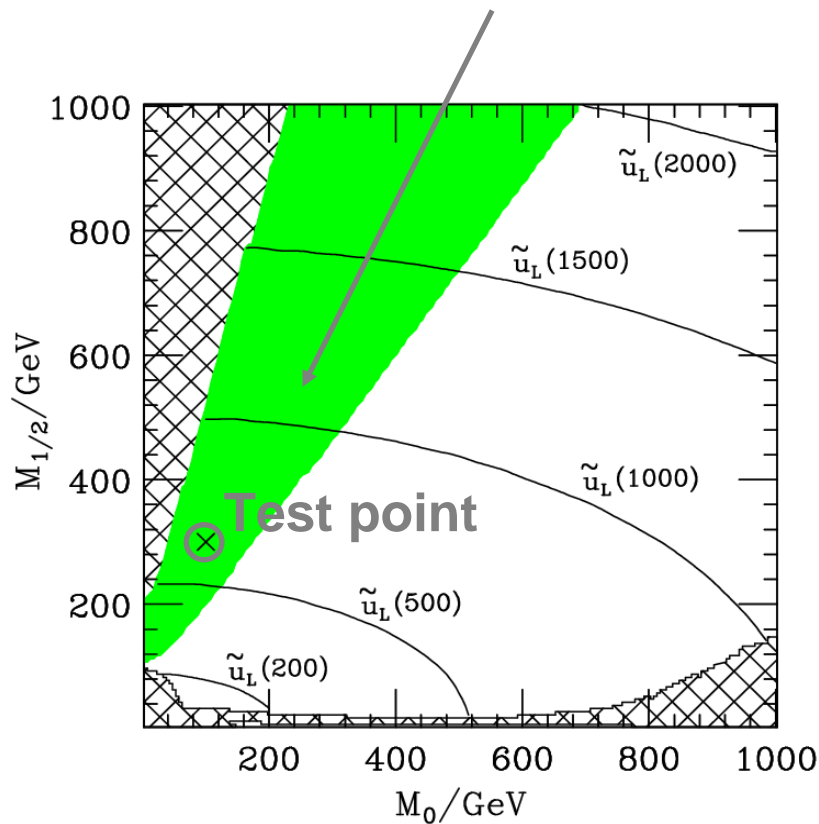
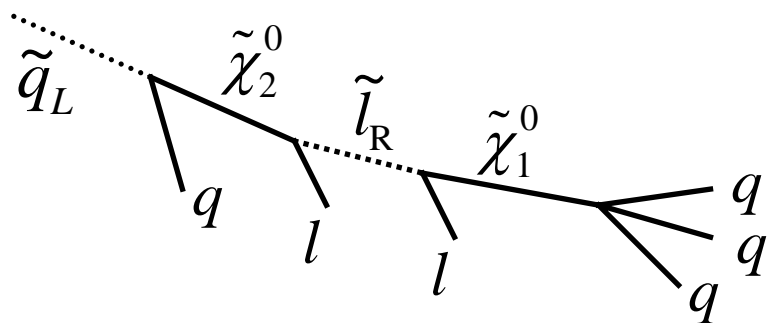




R-Parity Violation

- Use extra information from leptons to decrease background.
- Sequential decay of \tilde{q}_L to $\tilde{\chi}_1^0$ through $\tilde{\chi}_2^0$ and \tilde{l}_R producing Opposite Sign, Same Family (OSSF) leptons

Decay via \tilde{l}_R allowed where $m(\tilde{\chi}_2^0) > m(\tilde{l}_R)$

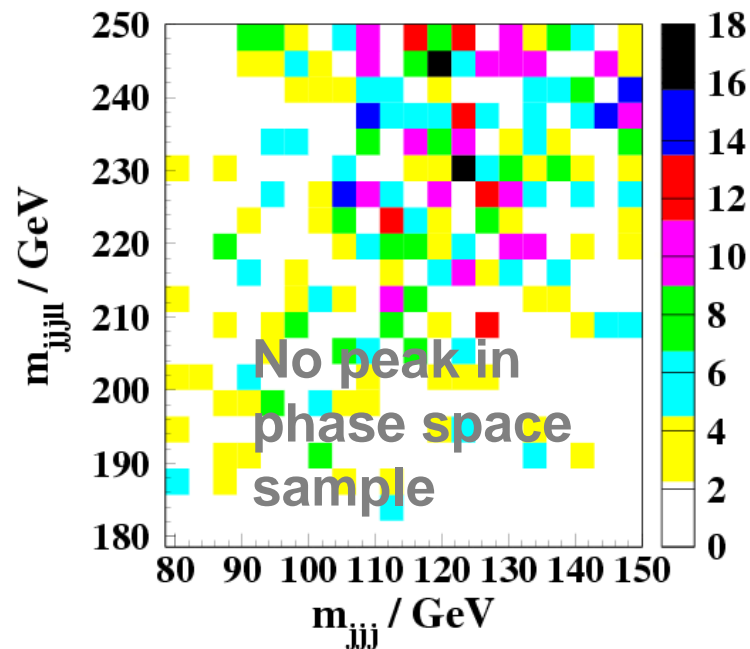
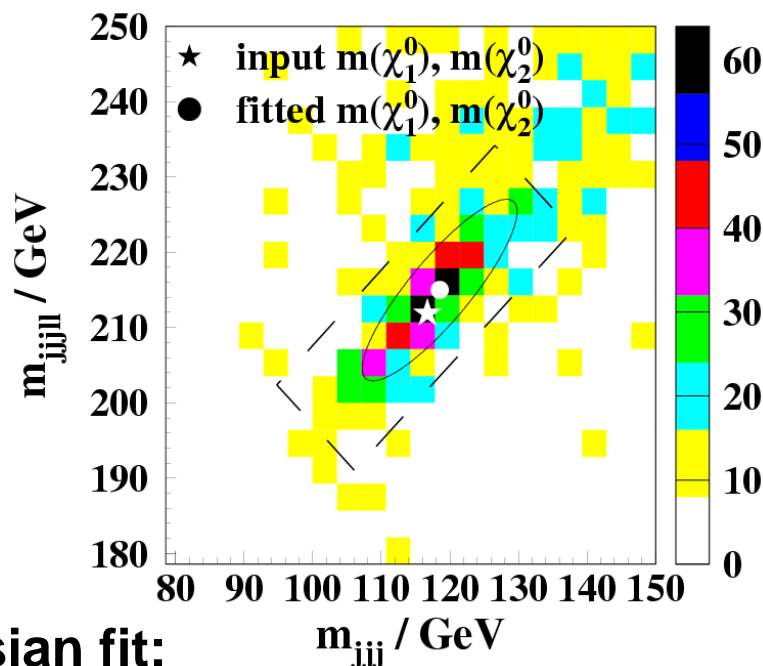




R-Parity Violation



- Perform simultaneous (2D) fit to 3jet and 3jet + 2lepton combination (measures mass of $\tilde{\chi}_2^0$).



Gaussian fit:

$$m(\tilde{\chi}_1^0) = 118.9 \pm 3 \text{ GeV}, (116.7 \text{ GeV})$$

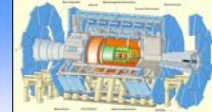
$$m(\tilde{\chi}_2^0) = 218.5 \pm 3 \text{ GeV} (211.9 \text{ GeV})$$

- Jet energy scale uncertainty $\approx 3\%$
 $\Rightarrow 3 \text{ GeV}$ systematic

- Can also measure squark and slepton masses.



R-Parity Violation



- Different λ''_{ijk} RPV couplings cause LSP decays to different quarks:

$$\tilde{\chi}_1^0 \rightarrow q_1 q_2 q_3$$

- Identifying the dominant λ'' gives insight into flavour structure of model.
- Use vertexing and non-isolated muons to statistically separate c - and b - from light quark jets.
- Remaining ambiguity from $d \rightarrow s$
- Dominant coupling could be identified at $> 3.5 \sigma$

Distinguishing		Vertexing		Muons		Combined
λ''_{ijk} from λ''_{lmn}		χ^2/df	P / %	χ^2/df	P / %	σ
uds	udb	59.1/1	-	28.7/1	-	9.4
	usb	73.0/1	-	31.7/1	-	10.2
	cds	30.5/1	-	4.0/1	4	5.9
	cdb	106.9/1	-	47.2/1	-	12.4
udb	csb	113.4/1	-	49.2/1	-	12.8
	usb	1.6/2	44	0.4/1	54	1.4
	cds	10.3/2	1	13.0/1	-	4.8
	cdb	18.3/2	-	6.8/2	3	5
usb	csb	16.3/2	-	5.1/2	8	4.6
	cds	17.5/2	-	17.2/1	-	5.9
	cdb	12.1/2	-	5.1/1	2	4.2
	csb	9.9/2	1	3.1/1	8	3.6
cds	cdb	56.1/2	-	37.4/1	-	9.7
	csb	55.8/2	-	35.3/1	-	9.5
cdb	csb	0.6/2	72	1.3/2	51	1.4